

# Lesson 1 - The Concept of a Function

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Essential Questions:

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## Example 1:

Suppose a moving object travels 256 feet in 4 seconds. Assume that the object travels at a constant speed; that is, the motion of the object is linear with a constant rate of change.

Number of seconds ( $x$ )	Distance traveled in feet ( $y$ )
1	
2	
3	
4	

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Write a linear equation in two variables to represent the situation, and use it to make predictions about the distance traveled over various intervals of time.

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What predictions does this equation allow us to make?

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Example 2:

The object, a stone, is dropped from a height of 256 feet. It takes exactly 4 seconds for the stone to hit the ground.

Number of seconds ( $x$ )	Distance traveled in feet ( $y$ )
1	
2	
3	
4	

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How far does the stone drop in the first 3 seconds?

What about the last 3 seconds?

Can we assume constant speed in this situation?

That is, can this situation be expressed using a linear equation?

[http://www.youtube.com/watch?v=KrX\\_zLuwOvc](http://www.youtube.com/watch?v=KrX_zLuwOvc)

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Draw a graph of the ball drop here.

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<p>Choose a prediction that was made about the distance traveled before we learned more about the situation. Was it accurate? How do you know?</p>	
<p>According to the data, how many feet did the stone drop in 3 seconds?</p>	
<p>After 1 second, how far had the stone dropped?</p>	
<p>After 3.5 seconds, how far had the stone dropped?</p>	

## On Your Own

Use the table to answer Exercises 1-5.

Number of seconds ( $x$ )	Distance traveled in feet ( $y$ )
0.5	4
1	16
1.5	36
2	64
2.5	100
3	144
3.5	196
4	256

1. Name two predictions you can make from this table.
  
2. Name a prediction that would require more information.
  
3. What is the average speed of the object between 0 and 3 seconds? How does this compare to the average speed calculated over the same interval in Example 1?

$$\text{Average Speed} = \frac{\text{distance traveled over a given time interval}}{\text{time interval}}$$

4. Take a closer look at the data for the falling stone by answering the questions below.
  - a. How many feet did the stone drop between 0 and 1 second?

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- b. How many feet did the stone drop between 1 and 2 seconds?

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c. How many feet did the stone drop between 2 and 3 seconds?

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d. How many feet did the stone drop between 3 and 4 seconds?

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e. Compare the distances the stone dropped from one time interval to the next. What do you notice?

5. What is the average speed of the stone in each interval 0.5 second? For example, the average speed over the interval from 3.5 seconds to 4 seconds is

$$\frac{\text{distance traveled over a given time interval}}{\text{time interval}} = \frac{256 - 196}{4 - 3.5} = \frac{60}{0.5} = 120 \text{ feet per second}$$

Repeat this process for every half-second interval. Then answer the question that follows.

a. Interval between 0 and 0.5 second:

b. Interval between 0.5 and 1 second:

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c. Interval between 1 and 1.5 seconds:

d. Interval between 1.5 and 2 seconds:

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e. Interval between 2 and 2.5 seconds:

f. Interval between 2.5 and 3 seconds:

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g. Interval between 3 and 3.5 seconds:

h. Compare the average speed between each time interval. What do you notice?

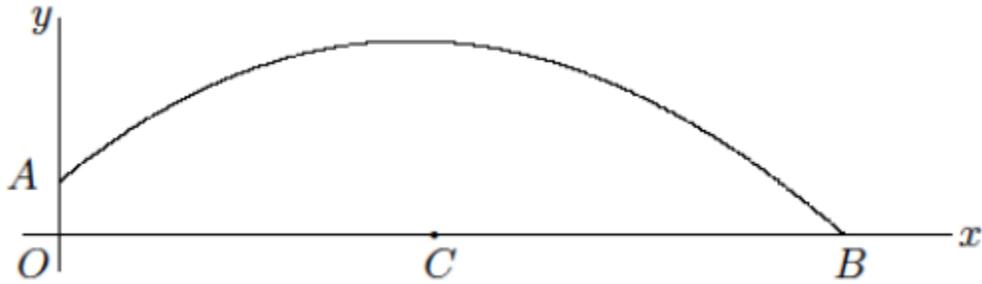
6. Is there any pattern to the data of the falling stone? Record your thoughts below.

Time of interval in seconds ( $t$ )	1	2	3	4
Distance stone fell in feet ( $y$ )	16	64	144	256

**Lesson 1 Summary:**

**Lesson 1 Independent Practice**

1. A ball is thrown across the field from point  $A$  to point  $B$ . It hits the ground at point  $B$ . The path of the ball is shown in the diagram below. The  $x$ -axis shows the distance the ball travels, and the  $y$ -axis shows the height of the ball. Use the diagram to complete parts (a)-(g).



a. Suppose  $A$  is approximately 6 feet above ground and that at time  $t = 0$  the ball is at point  $A$ . Suppose the length of  $OB$  is approximately 88 feet. Include this information on the diagram.

b. Suppose that after 1 second, the ball is at its highest point of 22 feet (above point  $C$ ) and has traveled a distance of 44 feet. Approximate the coordinates of the ball at the following values of  $t$ : 0.25, 0.5, 0.75, 1, 1.25, 1.5, 1.75, and 2.

c. Use your answer from part (b) to write two predictions.

d. What is the meaning of the point  $(88, 0)$ ?

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e. Why do you think the ball is at point  $(0, 6)$  when  $t = 0$ ? In other words, why isn't the height of the ball 0?

f. Does the graph allow us to make predictions about the height of the ball at all points?

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2. In your own words, explain the purpose of a function and why it is needed.

## Lesson 2 - Formal Definition of a Function

Essential Questions:

Definition:

Function:

Classwork:

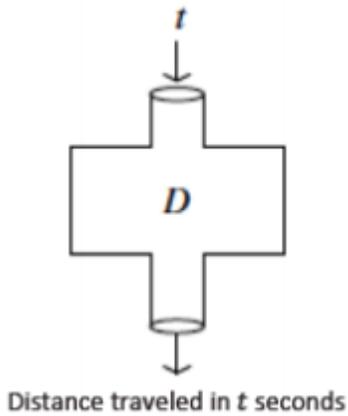
What do you notice between the two tables below?

Number of seconds ( $x$ )	Distance traveled in feet ( $y$ )
0.5	4
1	16
1.5	36
2	64
2.5	100
3	144
3.5	196
4	256

Number of seconds ( $x$ )	Distance traveled in feet ( $y$ )
0.5	4
1	4
1	36
2	64
2.5	80
3	99
3	196
4	256

$D$ assigns 4 to
$D$ assigns 16 to
$D$ assigns 36 to
$D$ assigns 64 to
$D$ assigns 100 to
$D$ assigns 144 to
$D$ assigns 196 to
$D$ assigns 256 to

**Input-Output Machine**



**On Your Own**

1. Let  $y$  be the distance traveled in time  $t$ . Use the function  $y = 16t^2$  to calculate the distance the stone dropped for the given time  $t$ .

Time of interval in seconds ( $t$ )	0.5	1	1.5	2	2.5	3	3.5	4
Distance stone fell in feet ( $y$ )								

a. Are the distances you calculated equal to the table from Lesson 1?

b. Does the function  $y = 16t^2$  accurately represent the distance the stone fell after a given time  $t$ ? In other words, does the function assign to  $t$  the correct distance? Explain.

**Definition-In your own words**

**Function:**

**On Your Own**

2. Can the table shown represent values of a function? Explain.

Input (x)	1	3	5	5	9
Output (y)	7	16	19	20	28

3. Can the table shown represent values of a function? Explain.

Input (x)	0.5	7	7	12	15
Output (y)	1	15	10	23	30

4. Can the table shown represent values of a function? Explain.

Input (x)	10	20	50	75	90
Output (y)	32	32	156	240	288

5. It takes Josephine 34 minutes to complete her homework assignment of 10 problems. If we assume that she works at a constant rate, we can describe the situation using a function.

a. Predict how many problems Josephine can complete in 25 minutes.

b. Write the two-variable linear equation that represents Josephine's constant rate of work.

c. Use the equation you wrote in part (b) as the formula for the function to complete the table below. Round your answers to the hundredths place.

Time taken to complete problems ( $x$ )	5	10	15	20	25
Number of problems completed ( $y$ )	1.47				

d. Compare your prediction from part (a) to the number you found in the table above.

e. Use the formula from part (b) to compute the number of problems completed when  $x = -7$ .

Does your answer make sense?

Explain.

f. For this problem, we assumed that Josephine worked at a constant rate.

Do you think that is a reasonable assumption for this situation?

Explain.

**Lesson 2 Summary**

## Lesson 2 Independent Practice

1. The table below represents the number of minutes Francisco spends at the gym each day for a week. Does the data shown below represent values of a function? Explain.

Day ( $x$ )	1	2	3	4	5	6	7
Time in minutes ( $y$ )	35	45	30	45	35	0	0

2. Can the table shown below represent values of a function? Explain.

Input ( $x$ )	9	8	7	8	9
Output ( $y$ )	11	15	19	24	28

3. Olivia examined the table of values shown below and stated that a possible rule to describe this function could be  $y = -2x + 9$ . Is she correct? Explain.

Input ( $x$ )	-4	0	4	8	12	16	20	24
Output ( $y$ )	17	9	1	-7	-15	-23	-31	-39

4. Peter said that the set of data in part (a) describes a function, but the set of data in part (b) does not. Do you agree? Explain why or why not.

a.

Input ( $x$ )	1	2	3	4	5	6	7	8
Output ( $y$ )	8	10	32	6	10	27	156	4

b.

Input ( $x$ )	-6	-15	-9	-3	-2	-3	8	9
Output ( $y$ )	0	-6	8	14	1	2	11	41

5. A function can be described by the rule  $y = x^2 + 4$ . Determine the corresponding output for each given input.

Input ( $x$ )	-3	-2	-1	0	1	2	3	4
Output ( $y$ )								

6. Examine the data in the table below. The inputs and outputs represent a situation where constant rate can be assumed. Determine the rule that describes the function.

Input ( $x$ )	-1	0	1	2	3	4	5	6
Output ( $y$ )	3	8	13	18	23	28	33	38

7. Examine the data in the table below. The inputs represent the number of bags of candy purchased, and the outputs represent the cost. Determine the cost of one bag of candy, assuming the price per bag is the same no matter how much candy is purchased. Then, complete the table.

Bags of candy ( $x$ )	1	2	3	4	5	6	7	8
Cost ( $y$ )				\$5.00	\$6.25			\$10.00

a. Write the rule that describes the function.

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b. Can you determine the value of the output for an input of  $x = -4$ ? If so, what is it?

c. Does an input of  $-4$  make sense in this situation? Explain.

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8. A local grocery store sells 2 pounds of bananas for \$1.00. Can this situation be represented by a function? Explain.

9. Write a brief explanation to a classmate who was absent today about why the table in part (a) is a function and the table in part (b) is not.

a.

Input ( $x$ )	-1	-2	-3	-4	4	3	2	1
Output ( $y$ )	81	100	320	400	400	320	100	81

b.

Input ( $x$ )	1	6	-9	-2	1	-10	8	14
Output ( $y$ )	2	6	-47	-8	19	-2	15	31

## Lesson 3 - Linear Functions and Proportionality

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Essential Questions:

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Example 1:

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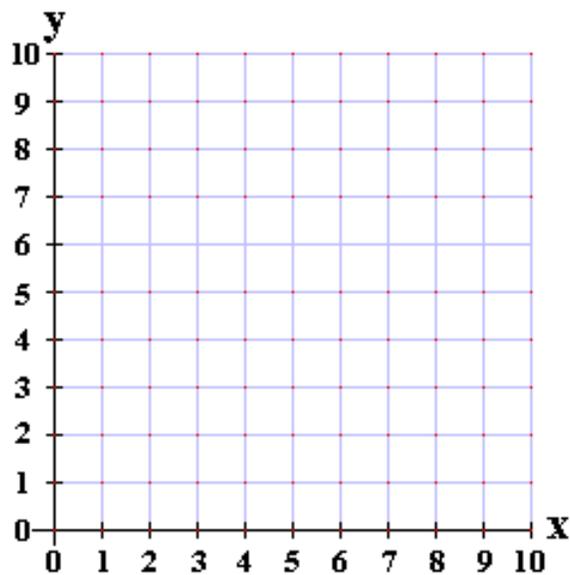
Bags of candy ( $x$ )	1	2	3	4	5	6	7	8
Cost ( $y$ )	\$1.25	\$2.50	\$3.75	\$5.00	\$6.25	\$7.50	\$8.75	\$10.00

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Do you think the table represents a linear function?

Justify your answer.

Graph the table data:



What rule or equation describes this function?

Would it make sense for  $x$  to ever be a negative number?

Why or why not?

Would you say the table represents all possible inputs and outputs?  
Explain

**Example 2:**

Walter walks 8 miles in 2 hours.  
What is his average speed?

Describe the function in this example.

What limitations do we need to put on  $x$ ?

**Example 3:**

Veronica runs at a constant speed. The distance she runs is a function of the time she spends running. The function has the table of values shown below.

Time in minutes ( $x$ )	8	16	24	32
Distance run in miles ( $y$ )	1	2	3	4

What rule or equation describes this function?

Using words, describe the function.

What limitations do we need to put on  $X$ ?

**Example 4:**

Water flows from a faucet at a constant rate. That is, the volume of water that flows out of the faucet is the same over any given time interval.

If 7 gallons of water flow from the faucet every 2 minutes, determine the rule that describes the volume function of the faucet.

Assume that the faucet is filling a bathtub that can hold 50 gallons of water. How long will it take the faucet to fill the tub?

Now assume that you are filling the same tub (a tub with a volume of 50 gallons) with the same faucet (a faucet where the rate of water flow is 3.5 gallons per minute).

This time, however, the tub already has 8 gallons in it.

Will it still take 14 minutes to fill the tub? Explain.

Generate a table of values for this function:

Time in minutes ( $x$ )	0	3	6	9	12
Total volume in tub in gallons ( $y$ )					

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**Example 5:**

Water flows from a faucet at a constant rate. Assume that 6 gallons of water are already in a tub by the time we notice the faucet is on. This information is recorded as 0 minutes and 6 gallons of water in the table below. The other values show how many gallons of water are in the tub at the given number of minutes.

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Time in minutes ( $x$ )	0	3	5	9
Total volume in tub in gallons ( $y$ )	6	9.6	12	16.8

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After 3 minutes there are 9.6 gallons of water in the tub. How much water flowed from the faucet in those 3 minutes?

What is the flow of water?

Write the volume of water flow as a function of time that represents the rate of water flow from the faucet.

Write the rule or equation that describes the volume of water flow as a function of time for tilling the tub, including the 6 gallons that were already in the tub.

How many minutes was the faucet on before we noticed it?  
Explain.

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**On Your Own**

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1. A linear function has the table of values below. The information in the table shows the function of time in minutes with respect to mowing an area of lawn in square feet.

Number of minutes ( $x$ )	5	20	30	50
Area mowed in square feet ( $y$ )	36	144	216	360

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a. Explain why this is a linear function.

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b. Describe the function in terms of area mowed and time.

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c. What is the rate of mowing a lawn in 5 minutes?

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d. What is the rate of mowing a lawn in 20 minutes?

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e. What is the rate of mowing a lawn in 30 minutes?

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<p>f. What is the rate of mowing a lawn in 50 minutes?</p>	
<p>g. Write the rule that represents the linear function that describes the area in square feet mowed, <math>y</math>, in <math>x</math> minutes.</p>	
<p>h. Describe the limitations of <math>x</math> and <math>y</math>.</p>	
<p>i. What number does the function assign to 24? That is, what area of lawn can be mowed in 24 minutes?</p>	
<p>j. How many minutes would it take to mow an area of 400 square feet?</p>	

2. A linear function has the table of values below. The information in the table shows the volume of water that flows from a hose in gallons as a function of time in minutes.

Time in minutes ( $x$ )	10	25	50	70
Total volume of water in gallons ( $y$ )	44	110	220	308

a. Describe the function in terms of volume and time.	
b. Write the rule that represents the linear function that describes the volume of water in gallons, $y$ , in $x$ minutes.	
c. What number does the function assign to 250? That is, how many gallons of water flow from the hose in 250 minutes?	
c. What number does the function assign to 250? That is, how many gallons of water flow from the hose in 250 minutes?	
e. Approximately how much time, in hours, will it take to finish filling the pool?	

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3. Recall that a linear function can be described by a rule in the form of  $y = mx + b$ , where  $m$  and  $b$  are constants. A particular linear function has the table of values below.

Input ( $x$ )	0	4	10	11	15	20	23
Output ( $y$ )	4	24	54	59			

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a. What is the equation that describes the function?

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b. Complete the table using the rule.

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**Summary:**

### Lesson 3 Independent Practice

1. A food bank distributes cans of vegetables every Saturday. They keep track of the cans in the following manner in the table. A linear function can be used to represent the data. The information in the table shows the function of time in weeks to the number of cans of vegetables distributed by the food bank.

Number of weeks ( $x$ )	1	12	20	45
Number of cans of vegetables distributed ( $y$ )	180	2,160	3,600	8,100

a. Describe the function in terms of cans distributed and time.

b. Write the equation or rule that represents the linear function that describes the number of cans handed out,  $y$ , in  $x$  weeks.

c. Assume that the food bank wants to distribute 20,000 cans of vegetables. How long will it take them to meet that goal?

d. Assume that the food bank has already handed out 35,000 cans of vegetables and continues to hand out cans at the same rate each week. Write a linear function that accounts for the number of cans already handed out.

e. Using your function in part (d), determine how long in years it will take the food bank to hand out 80,000 cans of vegetables.

2. A linear function has the table of values below. The information in the table shows the function of time in hours to the distance an airplane travels in miles. Assume constant speed.

Number of hours traveled ( $x$ )	2.5	4	4.2
Distance in miles ( $y$ )	1,062.5	1,700	1,785

a. Describe the function in terms of distance and time.

b. Write the rule that represents the linear function that describes the distance traveled in miles,  $y$ , in  $x$  hours.

c. Assume that the airplane is making a trip from New York to Los Angeles, which is approximately 2,475 miles. How long will it take the airplane to get to Los Angeles?

d. The airplane flies for 8 hours. How many miles will it be able to travel in that time interval?

3. A linear function has the table of values below. The information in the table shows the function of time in hours to the distance a car travels in miles.

Number of hours traveled ( $x$ )	3.5	3.75	4	4.25
Distance in miles ( $y$ )	203	217.5	232	246.5

a. Describe the function in terms of distance and time.

b. Write the rule that represents the linear function that describes the distance traveled in miles,  $y$ , in  $x$  hours.

c. Assume that the person driving the car is going on a road trip that is 500 miles from the starting point. How long will it take the person to get to the destination?

d. Assume that a second car is going on the road trip from the same starting point and traveling at the same constant rate. However, this car has already driven 210 miles. Write the rule that represents the linear function that accounts for the miles already driven by this car.

e. How long will it take the second car to drive the remainder of the trip?

4. A particular linear function has the table of values below.

Input ( $x$ )	2	3	8	11	15	20	23
Output ( $y$ )	7	10		34		61	

a. What is the equation that describes the function?

b. Complete the table using the rule.

5. A particular linear function has the table of values below.

Input ( $x$ )	0	5	8	13	15	18	21
Output ( $y$ )	6	11	14		21		

a. What is the rule that describes the function?

b. Complete the table using the rule.

## Lesson 4 - More Examples of Functions

Essential Questions:

**Discussion:** In the past couple of lessons, we looked at several linear functions and the number that assigned by the functions in the form of a table.

Table A:

Bags of candy ( $x$ )	1	2	3	4	5	6	7	8
Cost ( $y$ )	\$1.25	\$2.50	\$3.75	\$5.00	\$6.25	\$7.50	\$8.75	\$10.00

Table B:

Number of seconds ( $x$ )	0.5	1	1.5	2	2.5	3	3.5	4
Distance traveled in feet ( $y$ )	4	16	36	64	100	144	196	256

For the function in Table A, we said that the rule that described the function was  $y = 1.25x$ , where  $x \geq 0$ .

With respect to Table B, the rule that describes this function was  $y = 16x^2$ . Does this problem require the same restrictions on  $x$  as the previous problem? Explain.

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**Example 1:**

If 4 copies of the same book cost \$256.00, what is the unit rate for the book?

What cost does the function assign to 3 books? 3.5 books?

We can use the rule that describes the cost function to determine the cost of 3.5 books, but does it make sense?

Is this a discrete rate problem or a continuous rate problem? Explain.

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**Example 2:**

Water flows from a faucet at a constant rate. That is, the volume of water that flows out of the faucet is the same over any given time interval. If 7 gallons of water flow from the faucet every 2 minutes, determine the rule that describes the volume function of the faucet.

What limitations are there on  $x$  and  $y$ ?

Would this rate be considered discrete or continuous? Explain.

**Example 3:**

You have just been served freshly made soup that is so hot that it cannot be eaten. You measure the temperature of the soup, and it is  $210^{\circ}\text{F}$ . Since  $212^{\circ}\text{F}$  is boiling, there is no way it can safely be eaten yet. One minute after receiving the soup, the temperature has dropped to  $203^{\circ}\text{F}$ . If you assume that the rate at which the soup cools is linear, write a rule that would describe the rate of cooling of the soup.

We want to know how long it will be before the temperature of soup is at more tolerable temperature of  $147^{\circ}\text{F}$ . The difference in temperature from  $210^{\circ}\text{F}$  to  $147^{\circ}\text{F}$  is  $63^{\circ}\text{F}$ . For what number  $x$  will our function assign 63?

What do you notice about the change in temperature from one minute to the next?

Would this function be described as discrete or continuous?

Time	Temperature
after 2 minutes	196
after 3 minutes	190
after 4 minutes	184
after 5 minutes	178
after 6 minutes	173
after 7 minutes	168
after 8 minutes	163
after 9 minutes	158

**Example 4:**

Consider the following function:  
There is a function  $G$  so that the function assigns to each input, the number of a particular player, an output, the player's height. For example, the function  $G$  assigns to the input 1 an output of 5' 11".

1	5'11"
2	5'4"
3	5'9"
4	5'6"
5	6'3"
6	6'8"
7	5'9"
8	5'10"
9	6'2"

The function of  $G$  assigns to the input 2 what output?

Could the function  $G$  also assign to player 2 a second output of 5'6"? Explain.

Can we classify this function as discrete or continuous? Explain.

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**On Your Own:**

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1. A linear function has the table of values below related to the number of buses needed for a field trip.

Number of students ( $x$ )	35	70	105	140
Number of buses ( $y$ )	1	2	3	4

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a. Write the linear function that represents the number of buses needed,  $y$ , for  $x$  number of students.

b. Describe the limitations of  $x$  and  $y$ .

c. Is the function discrete or continuous?

d. The entire eighth-grade student body of 321 students is going on a field trip. What number of buses does our function assign to 321 students? Explain.

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e. Some seventh-grade students are going on their own field trip to a different destination, but just 180 are attending. What number does the function assign to 180? How many buses will be needed for the trip?

f. What number does the function assign to 50? Explain what this means and what your answer means.

2. A linear function has the table of values below related to the cost of movie tickets.

Number of tickets ( $x$ )	3	6	9	12
Total cost ( $y$ )	\$27.75	\$55.50	\$83.25	\$111.00

a. Write the linear function that represents the total cost,  $y$ , for  $x$  tickets purchased.

b. Is the function discrete or continuous? Explain.

c. What number does the function assign to 4? What do the question and your answer mean?

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3. A function produces the following table of values.

Input	Output
Banana	Yellow
Cherry	Red
Orange	Orange
Tangerine	Orange
Strawberry	Red

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a. Can this function be described by a rule using numbers? Explain.

b. Describe the assignment of the function.

c. State an input and the assignment the function would give to its output.

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**Lesson 4 Summary:**

#### Lesson 4 Independent Practice

1. A linear function has the table of values below related to the total cost for gallons of gas purchased.

Number of gallons ( $x$ )	5.4	6	15	17
Total cost ( $y$ )	\$19.71	\$21.90	\$54.75	\$62.05

- Write the linear function that represents the total cost,  $y$ , for  $x$  gallons of gas.
- Describe the limitations of  $x$  and  $y$ .
- Is the function discrete or continuous?
- What number does the function assign to 20? Explain what your answer means.

2. A function has the table of values below. Examine the information in the table to answer the questions below.

<b>Input</b>	<b>Output</b>
one	3
two	3
three	5
four	4
five	4
six	3
seven	5

a. Describe the function.

b. What number would the function assign to the word eleven?

3. A linear function has the table of values below related to the total number of miles driven in a given time interval in hours.

Number of hours driven ( $x$ )	3	4	5	6
Total miles driven ( $y$ )	141	188	235	282

- a. Write the linear function that represents the total miles driven,  $y$ , for  $x$  number of hours.
- b. Describe the limitations of  $x$  and  $y$ .
- c. Is the function discrete or continuous?
- d. What number does the function assign to 8? Explain what your answer means.
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- e. Use the function to determine how much time it would take to drive 500 miles.

4. A function has the table of values below that gives temperatures at specific times over a period of 8 hours.

12:00 p.m.	92°F
1:00 p.m.	90.5°F
2:00 p.m.	89°F
4:00 p.m.	86°F
8:00 p.m.	80°F

- Is the function a linear function? Explain.
- Describe the limitations of  $x$  and  $y$ .
- Is the function discrete or continuous?
- Let  $y$  represent the temperature and  $x$  represent the number of hours from 12:00 p.m. Write a rule that describes the function of time on temperature.
- Check that the rule you wrote to describe the function works for each of the input and output values given in the table.

- f. Use the function to determine the temperature at 5:30 p.m.
- g. Is it reasonable to assume that this function could be used to predict the temperature for 10:00 a.m. the following day or a temperature at any time on a day next week? Give specific examples in your explanation.

## Lesson 5 - Graphs of Functions and Equations

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Essential Questions:

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On Your Own:

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1. The distance that *Giselle* can run is a function of the amount of time she spends running. *Giselle* runs 3 miles in 21 minutes. Assume she runs at a constant rate.

a. Write an equation in two variables that represents her distance run,  $y$ , as a function of the time,  $x$ , she spends running.

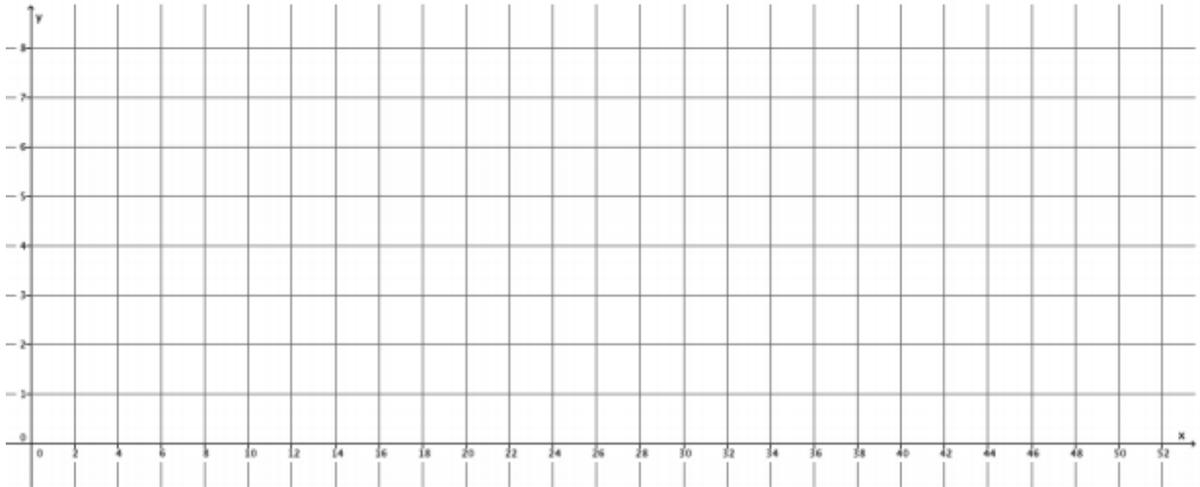
b. Use the equation you wrote in part (a) to determine how many miles *Giselle* can run in 14 minutes.

c. Use the equation you wrote in part (a) to determine how many miles *Giselle* can run in 28 minutes.

d. Use the equation you wrote in part (a) to determine how many miles *Giselle* can run in 7 minutes.

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e. The input of the function,  $x$ , is time, and the output of the function,  $y$ , is the distance Giselle ran. Write the inputs and outputs from parts (b)-(d) as ordered pairs, and plot them as points on a coordinate plane.



f. What shape does the graph of the points appear to take?

g. Is the function continuous or discrete?

h. Use the equation you wrote in part (a) to determine how many miles Giselle can run in 36 minutes. Write your answer as an ordered pair, as you did in part (e), and include the point on the graph. Is the point in a place where you expected it to be? Explain.

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i. Assume you used the rule that describes the function to determine how many miles Giselle can run for any given time and wrote each answer as an ordered pair. Where do you think these points would appear on the graph?

j. What do you think the graph of this function will look like? Explain.

k. Connect the points you have graphed to make a line. Select a point on the graph that has integer coordinates. Verify that this point has an output that the function would assign to the input.

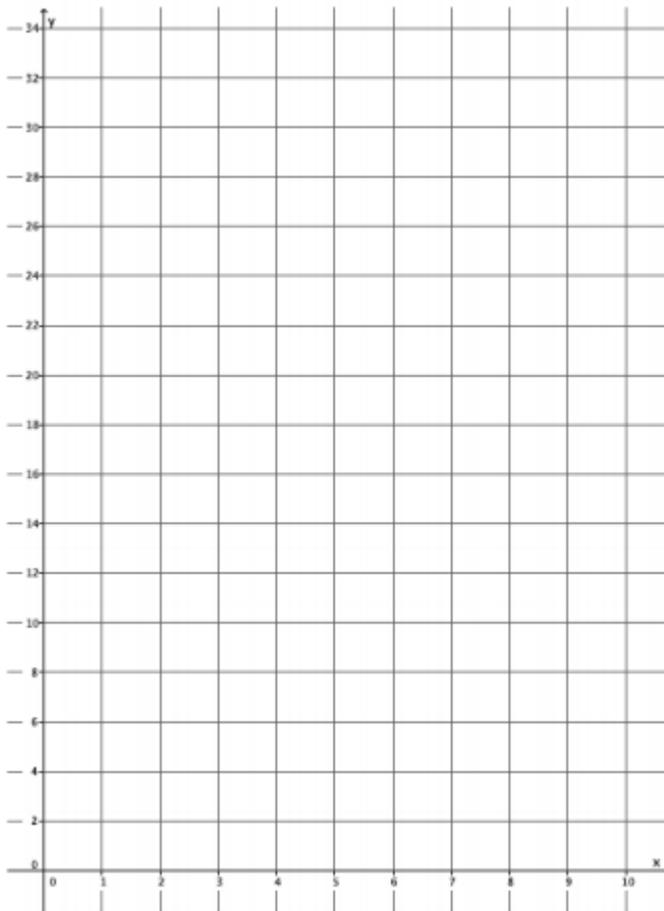
I. Sketch the graph of the equation  $y = \frac{1}{7}x$  using the same coordinate plane in part (e). What do you notice about the graph of the function that describes Giselle's constant rate of running and the graph of the equation  $y = \frac{1}{7}x$ ?

---

2. Sketch the graph of the equation  $y = x^2$  for positive values of  $x$ . Organize your work using the table below, and then answer the questions that follow.

$x$	$y$
0	
1	
2	
3	
4	
5	
6	

a. Plot the ordered pairs on the coordinate plane.



---

b. What shape does the graph of the points appear to take?

c. Is this equation a linear equation? Explain.

d. An area function  $A$  for a square with length of a side  $s$  has the rule so that it assigns to each input an output, the area of the square,  $A$ . Write the rule for this function.

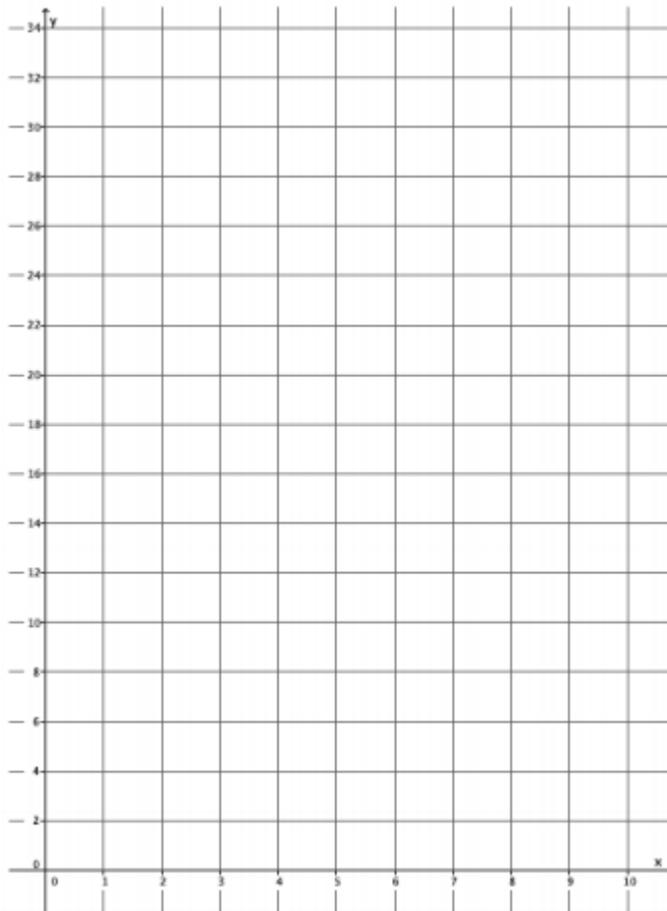
e. What do you think the graph of this function will look like? Explain.

f. Use the function you wrote in part (d) to determine the area of a square with side length 2.5. Write the input and output as an ordered pair. Does this point appear to belong to the graph of  $y = x^2$ ?

<p>3. The number of devices a particular manufacturing company can produce is a function of the number of hours spent making the devices. On average, 4 devices are produced each hour. Assume that devices are produced at a constant rate.</p>	
<p>a. Write an equation in two variables that represents the number of devices, <math>y</math>, as a function of the time the company spends making the devices, <math>x</math>.</p>	
<p>b. Use the equation you wrote in part (a) to determine how many devices are produced in 8 hours.</p>	
<p>c. Use the equation you wrote in part (a) to determine how many devices are produced in 6 hours.</p>	

d. Use the equation you wrote in part (a) to determine how many devices are produced in 4 hours.

e. The input of the function,  $x$ , is time, and the output of the function,  $y$ , is the number of devices produced. Write the inputs and outputs from parts (b)-(d) as ordered pairs, and plot them as points on a coordinate plane.



f. What shape does the graph of the points appear to take?

---

g. Is the function continuous or discrete?

h. Use the equation you wrote in part (a) to determine how many devices are produced in 1.5 hours. Write your answer as an ordered pair, as you did in part (e), and include the point on the graph. Is the point in a place where you expected it to be? Explain.

i. Assume you used the rule that describes the function to determine how many devices are produced for any given time and wrote each answer as an ordered pair. Where do you think these points would appear on the graph?

j. What do you think the graph of this function will look like? Explain.

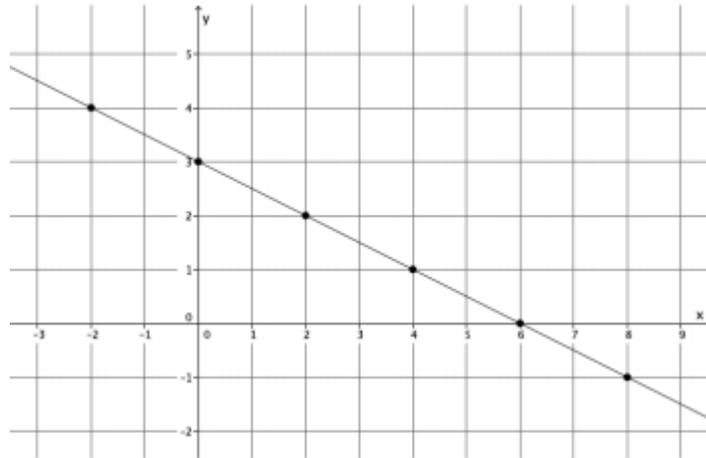
k. Connect the points you have graphed to make a line. Select a point on the graph that has integer coordinates. Verify that this point has an output that the function would assign to the input.

l. Sketch the graph of the equation  $y = 4x$  using the same coordinate plane in part (e). What do you notice about the graph of the function that describes the company's constant rate of producing devices and the graph of the equation  $y = 4x$ ?

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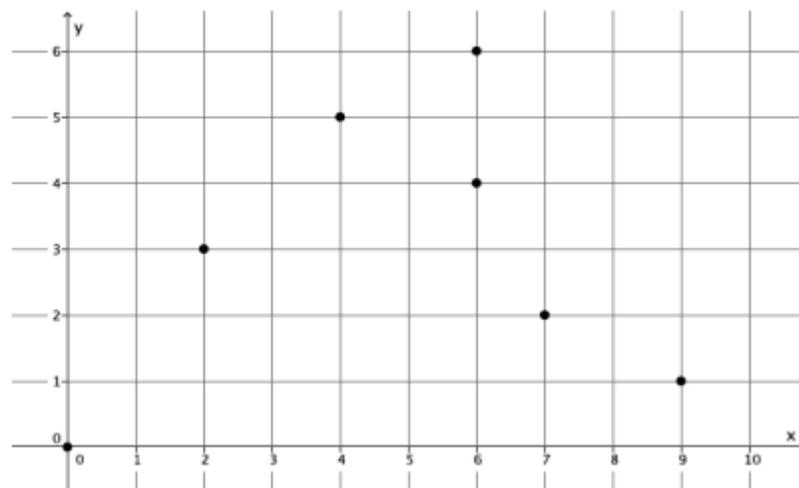
4. Examine the three graphs below. Which, if any, could represent the graph of a function? Explain why or why not for each graph.

Graph 1:



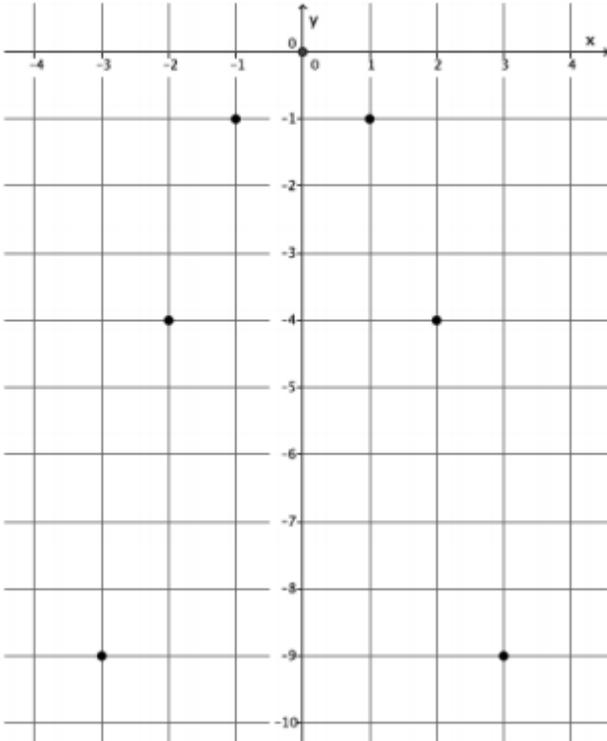
Explain.

Graph 2:



Explain.

Graph 3:



Explain.

Lesson 5 Summary:

### Lesson 5 Independent Practice

1. The distance that Scott walks is a function of the time he spends walking. Scott can walk  $\frac{1}{2}$  mile every 8 minutes. Assume he walks at a constant rate.

a. Predict the shape of the graph of the function. Explain.

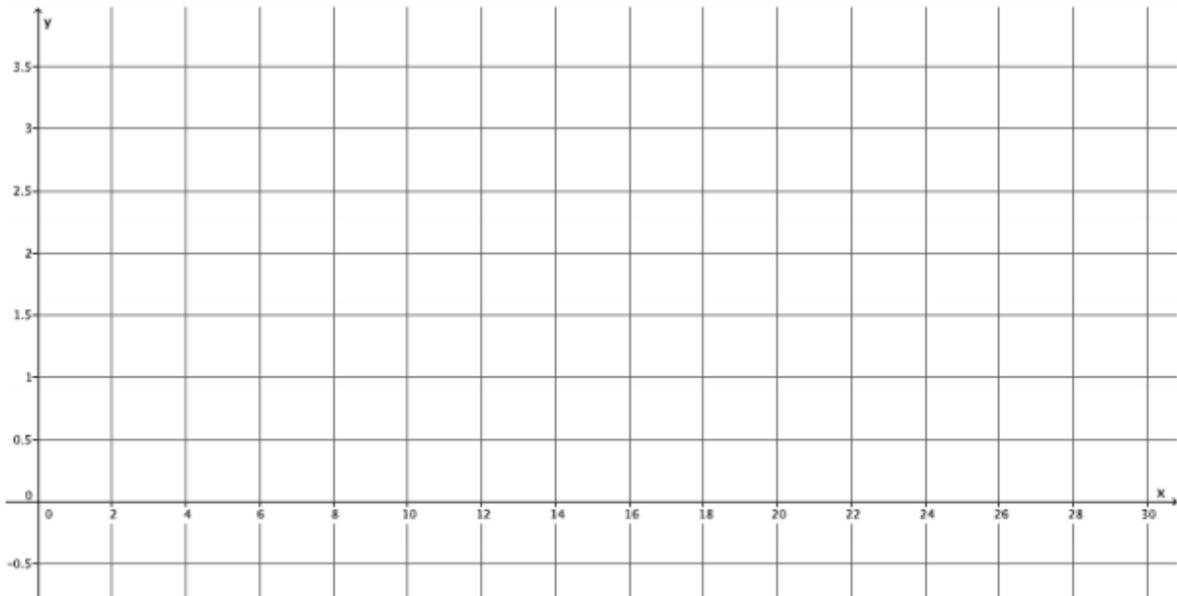
b. Write an equation to represent the distance that Scott can walk,  $y$ , in  $x$  minutes.

c. Use the equation you wrote in part (b) to determine how many miles Scott can walk in 24 minutes.

d. Use the equation you wrote in part (b) to determine how many miles Scott can walk in 12 minutes.

e. Use the equation you wrote in part (b) to determine how many miles Scott can walk in 16 minutes.

f. Write your inputs and corresponding outputs as ordered pairs, and then plot them on a coordinate plane.

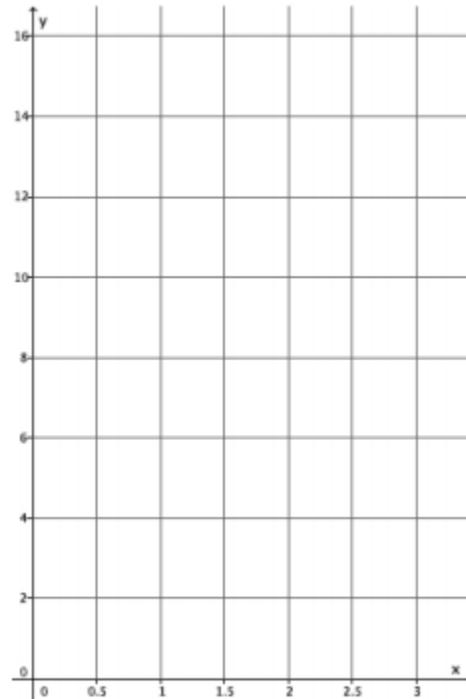


g. What shape does the graph of the points appear to take? Does it match your prediction?

h. If the function that represents Scott's walking is continuous, connect the points to make a line, and then write the equation that represents the graph of the function. What do you notice?

2. Graph the equation  $y = x^3$  for positive values of  $x$ . Organize your work using the table below, and then answer the questions that follow.

$x$	$y$
0	
0.5	
1	
1.5	
2	
2.5	



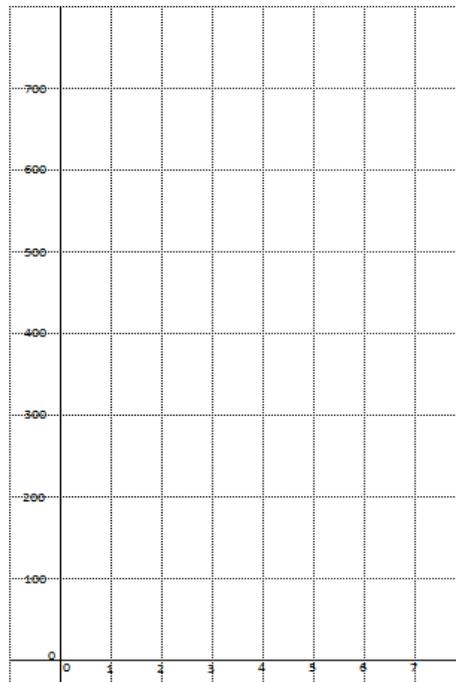
- Plot the ordered pairs on the coordinate plane.
- What shape does the graph of the points appear to take?
- Is this the graph of a linear function? Explain.

- d. A volume function has the rule so that it assigns to each input, the length of one side of a cube,  $s$ , and to the output, the volume of the cube,  $V$ . The rule for this function is  $V = s^3$ . What do you think the graph of this function will look like? Explain
- e. Use the function in part (d) to determine the volume with side length of 3. Write the input and output as an ordered pair. Does this point appear to belong to the graph of  $y = x^3$ ?

3. Sketch the graph of the equation  $y = 180(x - 2)$  for whole numbers. Organize your work using the table below, and then answer the questions that follow.

$x$	$y$
3	
4	
5	
6	

- a. Plot the ordered pairs on the coordinate plane.

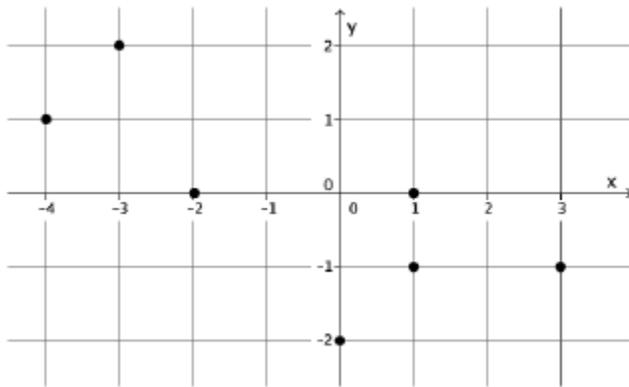


- b. What shape does the graph of the points appear to take?
- c. Is this graph a graph of a function? How do you know?
- d. Is this a linear equation? Explain.

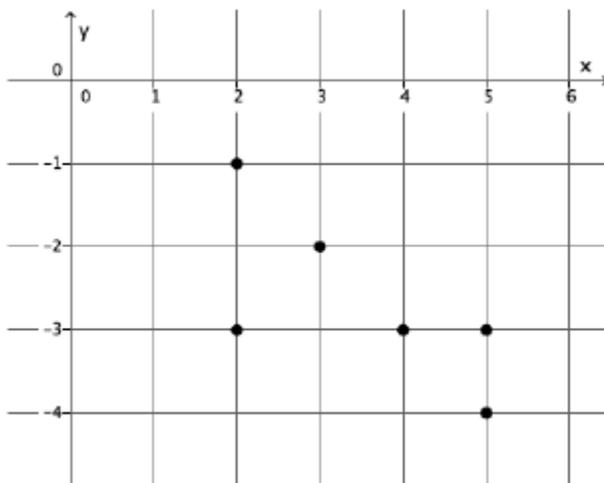
e. The sum of interior angles of a polygon has the rule so that it assigns each input, the number of sides,  $n$ , of the polygon, and to the output,  $S$ , the sum of the interior angles of the polygon. The rule for this function is  $S = 180(n - 2)$ . What do you think the graph of this function will look like? Explain.

f. Is this function continuous or discrete? Explain.

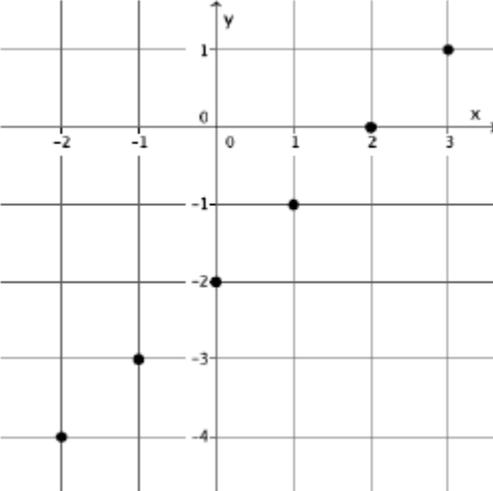
4. Examine the graph below. Could the graph represent the graph of a function? Explain why or why not.



5. Examine the graph below. Could the graph represent the graph of a function? Explain why or why not.



6. Examine the graph below. Could the graph represent the graph of a function? Explain why or why not.



## Lesson 6 - Graphs of Linear Functions and Rate of Change

Essential Questions:

Classwork:

Functions 1, 2, and 3 have the tables shown below. Examine each of them, make a conjecture about which will be linear, and justify your claim.

Input	Output
2	5
4	7
5	8
8	11

Input	Output
2	4
3	9
4	16
5	25

Input	Output
0	-3
1	1
2	6
3	9

Summarize your conjectures

Suppose a function can be described by an equation in the form of  $y = mx + b$  and that the function assigns the values shown in the table:

Input	Output
2	5
3.5	8
4	9
4.5	10

Compute the slope.

---

If the rate of change (that is, slope) is the same for each pair of inputs and outputs, then we know we are looking at a linear function.

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Calculate between rows  
2 and 3:

---

Calculate between rows  
3 and 4:

---

What did you notice?

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Now solve for b:

---

What is the equation?

---

What would the graph of this  
function look like?

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Is this function linear?

Input	Output
-2	4
3	9
4.5	20.25
5	25

If so, what equation describes the function?

What is the rate of change?  
Compare at least 3 different pairs of inputs and outputs.

1) \_\_\_\_\_

2) \_\_\_\_\_

3) \_\_\_\_\_

If this function were linear, what would we expect to see?

Tell about the graph of this line.

**On Your Own**

A function assigns the inputs and corresponding outputs shown in the table below.

Input	Output
1	2
2	-1
4	-7
6	-13

a. Is the function a linear function? Check at least three pairs of inputs and their corresponding outputs.

b. What equation describes the function?

c. What will the graph of the function look like? Explain.

**Lesson 6 Summary:**

**Lesson 6 Independent Practice**

1. A function assigns the inputs and corresponding outputs shown in the table below.

Input	Output
3	9
9	17
12	21
15	25

a. Is the function a linear function? Check at least three pairs of inputs and their corresponding outputs.

b. What equation describes the function?

c. What will the graph of the function look like? Explain.

2. A function assigns the inputs and corresponding outputs shown in the table below.

Input	Output
-1	2
0	0
1	2
2	8
3	18

a. Is the function a linear function?

b. What equation describes the function?

3. A function assigns the inputs and corresponding outputs shown in the table below.

Input	Output
0.2	2
0.6	6
1.5	15
2.1	21

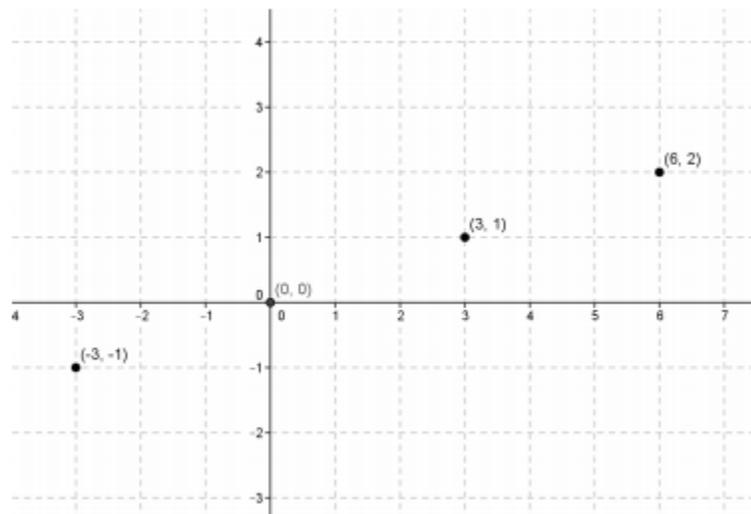
a. Is the function a linear function? Check at least three pairs of inputs and their corresponding outputs.

b. What equation describes the function?

c. What will the graph of the function look like? Explain.

4. Martin says that you only need to check the first and last input and output values to determine if the function is linear. Is he correct? Explain. Hint: Show an example with a table that is not a function.

5. Is the following graph a graph of a linear function? How would you determine if it is a linear function?



6. A function assigns the inputs and corresponding outputs shown in the table below.

Input	Output
-6	-6
-5	-5
-4	-4
-2	-2

a. Is the function a linear function? Check at least three pairs of inputs and their corresponding outputs.

b. What equation describes the function?

c. What will the graph of the function look like? Explain.

## Lesson 7 - Comparing Linear Functions and Graphs

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Essential Questions:

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### Exercises

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1. Alan and Margot drive from City A to City B, a distance of 147 miles. They take the same route and drive at constant speeds. Alan begins driving at 1:40 p.m. and arrives at City B at 4:15 p.m. Margot's trip from City A to City B can be described with the equation  $y = 64x$ , where  $y$  is the distance traveled and  $x$  is the time in minutes spent traveling.

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Who gets from City A to City B faster?	
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2. You have recently begun researching phone billing plans. Phone Company A charges a flat rate of \$75 a month. A flat rate means that your bill will be \$75 each month with no additional costs. The billing plan for Phone Company B is a linear function of the number of texts that you send that month. That is, the total cost of the bill changes each month depending on how many texts you send. The table represents the inputs and the corresponding outputs that the function assigns.

Input (number of texts)	Output (cost of bill)
50	\$50
150	\$60
200	\$65
500	\$95

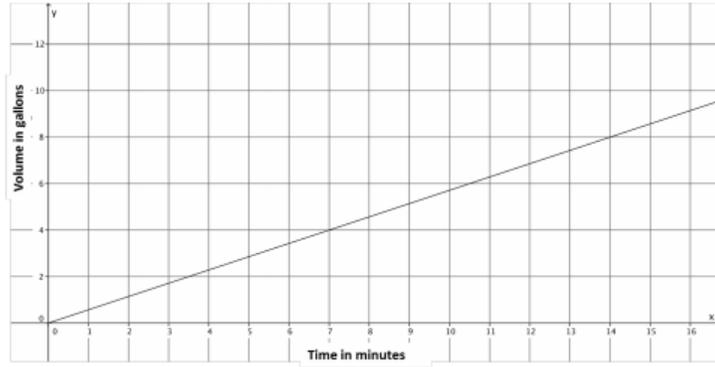
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At what number of texts would the bill from each phone plan be the same?

At what number of texts is Phone Company A the better choice?

At what number of texts is Phone Company B the better choice?

3. A function describes the volume of water,  $y$ , that flows from Faucet A in gallons for  $x$  minutes. The graph below is the graph of this linear function. Faucet B's water flow can be described by the equation  $y = \frac{5}{6}x$ , where  $y$  is the volume of water in gallons that flows from the faucet in  $x$  minutes. Assume the flow of water from each faucet is constant.



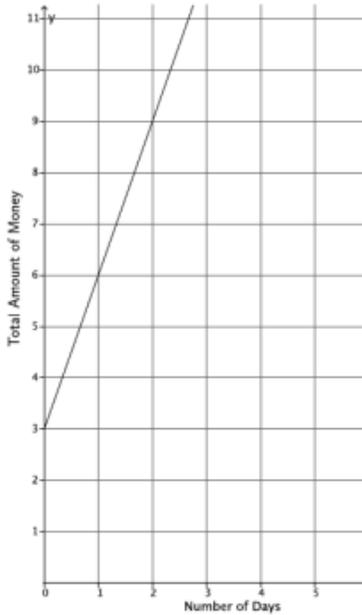
Which faucet has a faster rate of flow of water?

Each faucet is being used to fill tubs with a volume of 50 gallons. How long will it take each faucet to fill the tub? How do you know?

The tub that is filled by Faucet A already has 15 gallons in it. If both faucets are turned on at the same time, which faucet will fill its tub faster?

4. Two people, Adam and Bianca, are competing to see who can save the most money in one month. Use the table and the graph below to determine who will save more money at the end of the month. State how much money each person had at the start of the competition.

Adam's Savings:



Bianca's Savings:

Input (Number of Days)	Output (Total amount of money)
5	\$17
8	\$26
12	\$38
20	\$62

Analysis of Adam's savings:

Analysis of Bianca's savings:

**Discussion:**

Describe some of the methods of problem solving used by you or your classmates.

Was one method more efficient than another?

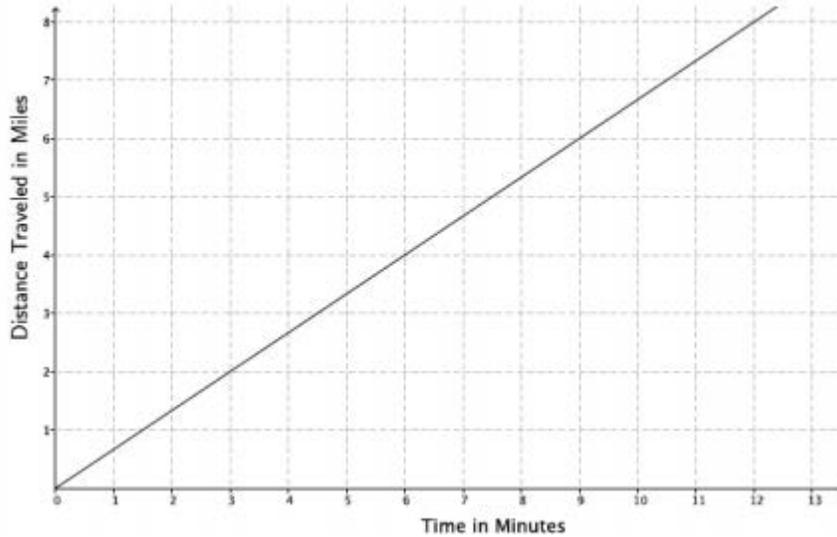
How did you know one method was more efficient than another?

**Lesson 7 Summary:**

### Lesson 7 Independent Practice

1. The graph below represents the distance,  $y$ , Car A travels in  $x$  minutes. The table represents the distance,  $y$ , Car B travels in  $x$  minutes. Which car is traveling at a greater speed? How do you know?

Car A:



Car B:

Time in minutes ( $x$ )	Distance ( $y$ )
15	12.5
30	25
45	37.5

2. The local park needs to replace an existing fence that is 6 feet high. Fence Company A charges \$7,000 for building materials and \$200 per foot for the length of the fence. Fence Company B charges based on the length of the fence. That is, the total cost of the six-foot high fence will depend on how long the fence is. The table below represents the inputs and the corresponding outputs that the function assigns for Fence Company B.

Input (length of fence)	Output (cost of bill)
100	\$26,000
120	\$31,200
180	\$46,800
250	\$65,000

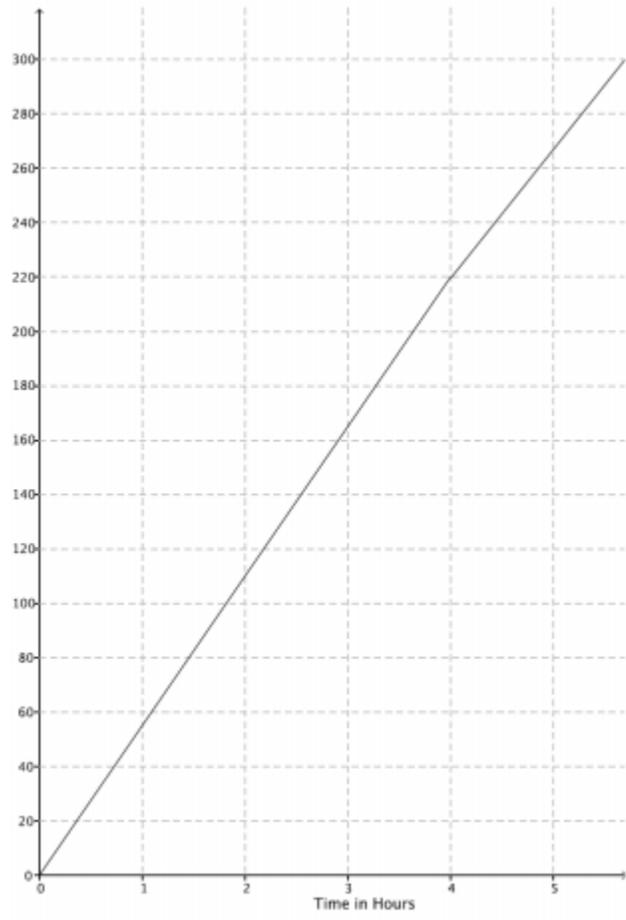
a. Which company charges a higher rate per foot of fencing? How do you know?

b. At what number of the length of the fence would the cost from each fence company be the same? What will the cost be when the companies charge the same amount? If the fence you need is 190 feet in length, which company would be a better choice?

3. The rule  $y = 123x$  is used to describe the function for the number of minutes needed,  $x$ , to produce  $y$  toys at Toys Plus. Another company, #1 Toys, has a similar function that assigned the values shown in the table below. Which company produces toys at a slower rate? Explain.

Time in minutes ( $x$ )	Toys Produced ( $y$ )
5	600
11	1,320
13	1,560

4. A function describes the number of miles a train can travel,  $y$ , for the number of hours,  $x$ . The figure shows the graph of this function. Assume that the train travels at a constant speed. The train is traveling from City A to City B (a distance of 320 miles). After 4 hours, the train slows down to a constant speed of 48 miles per hour.



a. How long will it take the train to reach its destination?

b. If the train had not slowed down after 4 hours, how long would it have taken to reach its destination?

c. Suppose after 4 hours, the train increased its constant speed. How fast would the train have to travel to complete the destination in 1.5 hours?

d. A hose is used to fill up a 1,200 gallon water truck at a constant rate. After 10 minutes, there are 65 gallons of water in the truck. After 15 minutes, there are 82 gallons of water in the truck. How long will it take to fill up the water truck?

e. The driver of the truck realizes that something is wrong with the hose he is using. After 30 minutes, he shuts off the hose and tries a different hose. The second hose has a constant rate of 18 gallons per minute. How long does it take the second hose to fill up the truck?

f. Could there ever be a time when the first hose and the second hose filled up the same amount of water?

5. a. A hose is used to fill up a 1,200 gallon water truck at a constant rate. After 10 minutes, there are 65 gallons of water in the truck. After 15 minutes, there are 82 gallons of water in the truck. How long will it take to fill up the water truck?

b. The driver of the truck realizes that something is wrong with the hose he is using. After 30 minutes, he shuts off the hose and tries a different hose. The second hose has a constant rate of 18 gallons per minute. How long does it take the second hose to fill up the truck?

c. Could there ever be a time when the first hose and the second hose filled up the same amount of water?

## Lesson 8 - Graphs of Simple Nonlinear Functions

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Essential Questions:

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Classwork/On Your Own:

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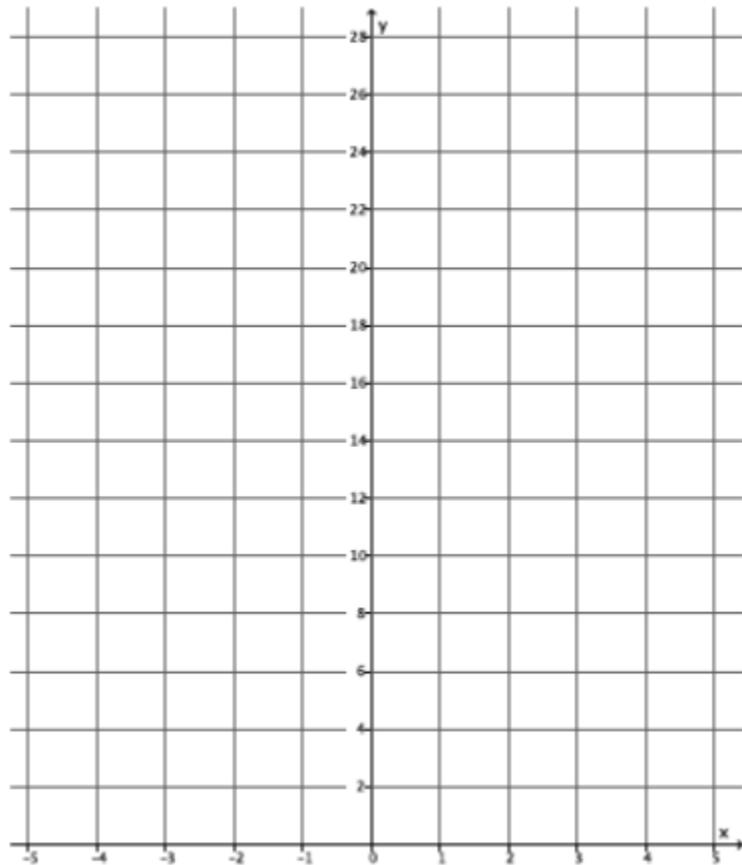
1. A function has the rule so that each input of  $x$  is assigned an output of  $x^2$ .

a. Do you think the function is linear or nonlinear? Explain.

b. Develop a list of inputs and outputs for this function. Organize your work using the table. Then, answer the questions that follow.

Input ( $x$ )	Output ( $x^2$ )
-5	
-4	
-3	
-2	
-1	
0	
1	
2	
3	
4	
5	

c. Plot the inputs and outputs as points on the coordinate plane where the output is the  $y$ -coordinate.



d. What shape does the graph of the points appear to take?

e. Find the rate of change using rows 1 and 2 from the table above.

f. Find the rate of change using rows 2 and 3 from the above table.

g. Find the rate of change using any two other rows from the above table.

h. Return to your initial claim about the function. Is it linear or nonlinear? Justify your answer with as many pieces of evidence as possible.

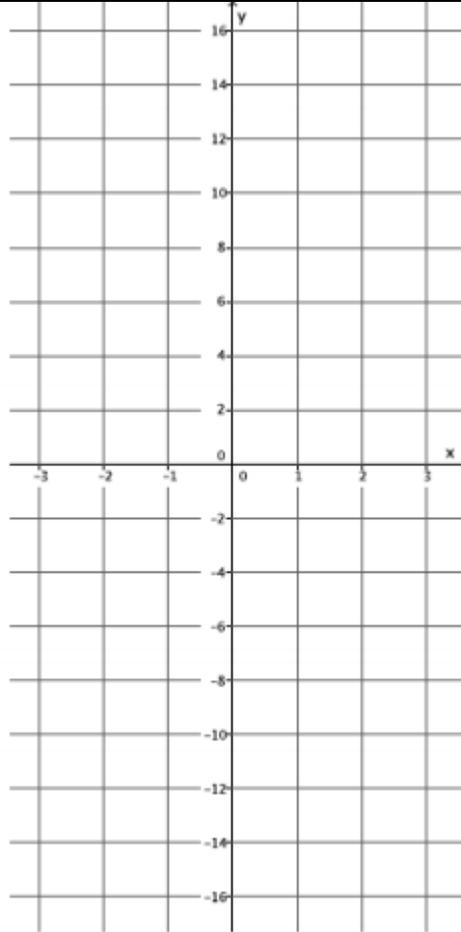
2. A function has the rule so that each input of  $x$  is assigned an output of  $x^3$ .

a. Do you think the function is linear or nonlinear? Explain.

b. Develop a list of inputs and outputs for this function. Organize your work using the table. Then, answer the questions that follow.

Input ( $x$ )	Output ( $x^3$ )
-2.5	
-2	
-1.5	
-1	
-0.5	
0	
0.5	
1	
1.5	
2	
2.5	

c. Plot the inputs and outputs as points on the coordinate plane where the output is the  $y$ -coordinate.



d. What shape does the graph of the points appear to take?

e. Find the rate of change using rows 2 and 3 from the table above.

f. Find the rate of change using rows 3 and 4 from the table above.

g. Find the rate of change using rows 8 and 9 from the table above.

h. Return to your initial claim about the function. Is it linear or nonlinear? Justify your answer with as many pieces of evidence as possible.

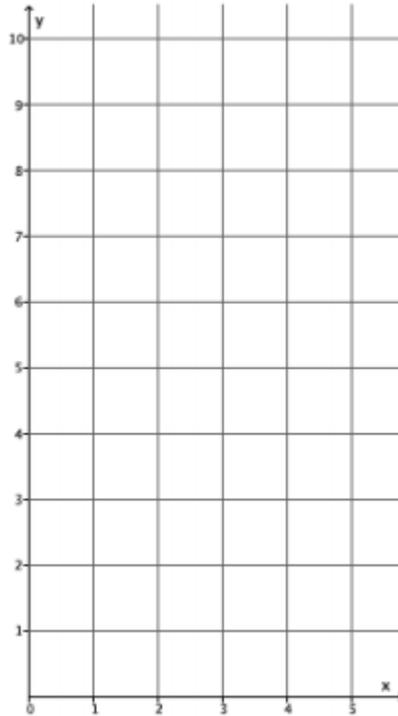
3. A function has the rule so that each input of  $x$  is assigned an output of  $\frac{1}{x}$  for values of  $x > 0$ .

a. Do you think the function is linear or nonlinear? Explain.

b. Develop a list of inputs and outputs for this function. Organize your work using the table. Then, answer the questions that follow.

Input ( $x$ )	Output ( $\frac{1}{x}$ )
0.1	
0.2	
0.4	
0.5	
0.8	
1	
1.6	
2	
2.5	
4	
5	

c. Plot the inputs and outputs as points on the coordinate plane where the output is the  $y$ -coordinate.



d. What shape does the graph of the points appear to take?

e. Find the rate of change using rows 1 and 2 from the table above.

f. Find the rate of change using rows 2 and 3 from the table above.

g. Find the rate of change using any two other rows from the table above.

h. Return to your initial claim about the function. Is it linear or nonlinear? Justify your answer with as many pieces of evidence as possible.

**Discussion:**

What did you notice about the rate of change in the last 3 problems?

What do we know about the function?

If we know that the rate of change is not the same for each input and output, what do we know about the function?

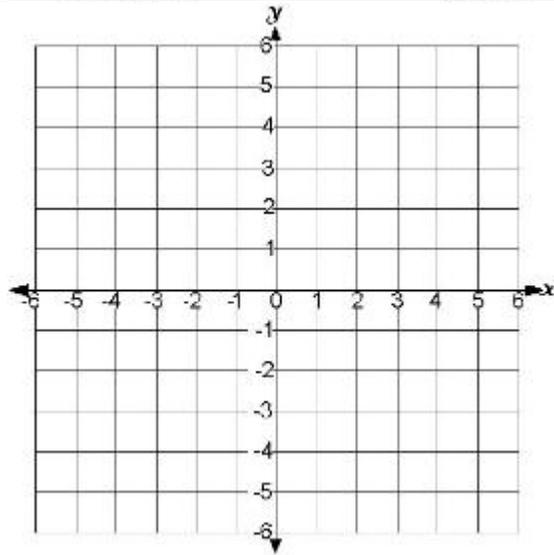
What did you notice about the exponent?

Is there another way to know that the equations are nonlinear?

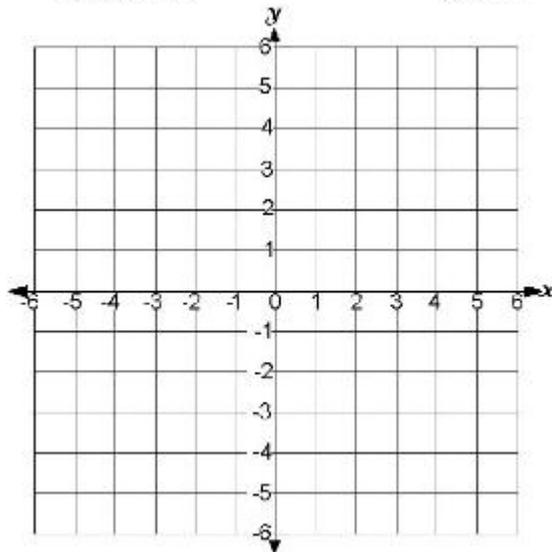
**On Your Own**

In Exercises 4-10, the rule that describes a function is given. If necessary, use a table to organize pairs of inputs and outputs, and then plot each on a coordinate plane to help answer the questions.

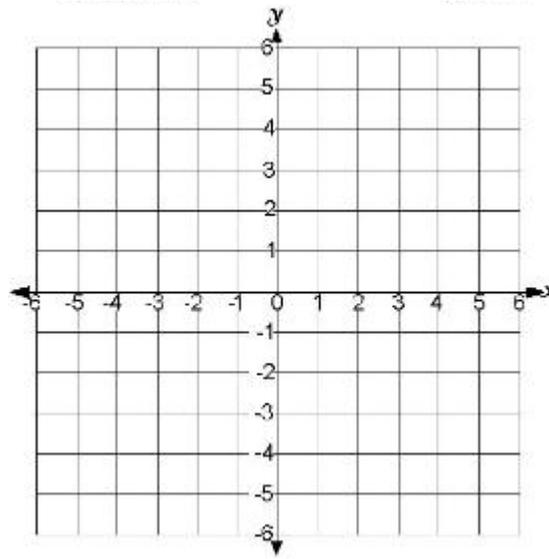
4. What shape do you expect the graph of the function described by  $y = x$  to take? Is it a linear or nonlinear function?



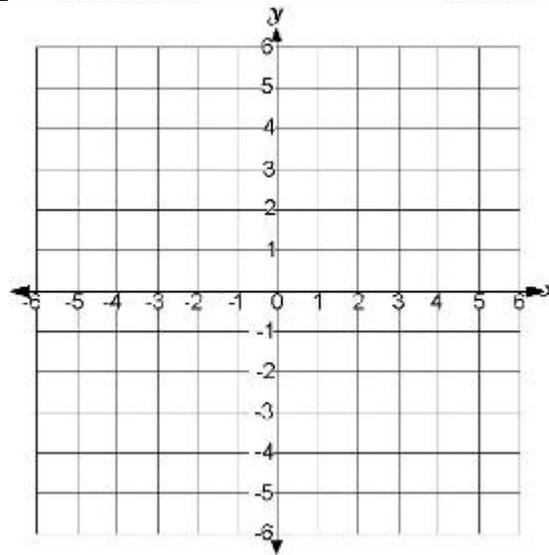
5. What shape do you expect the graph of the function described by  $y = 2x^2 - x$  to take? Is it a linear or nonlinear function?



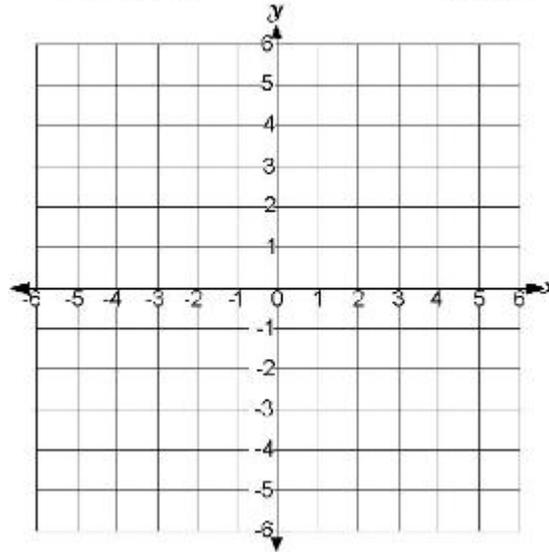
6. What shape do you expect the graph of the function described by  $3x + 7y = 8$  to take? Is it a linear or nonlinear function?



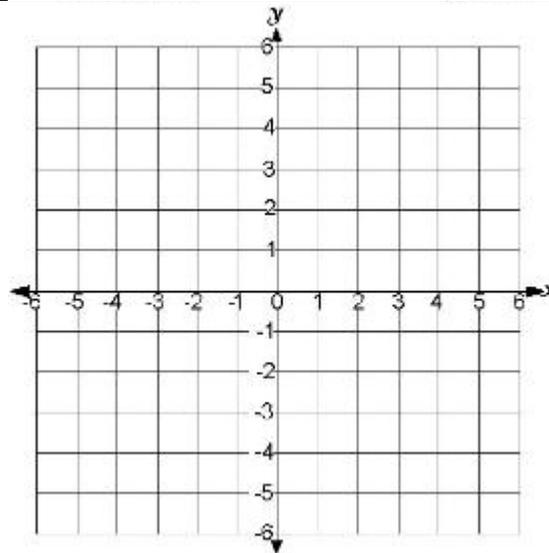
7. What shape do you expect the graph of the function described by  $y = 4x^3$  to take? Is it a linear or nonlinear function?



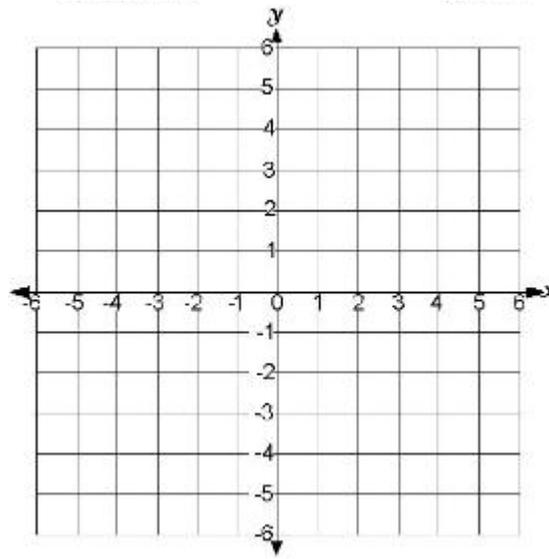
8. What shape do you expect the graph of the function described by  $\frac{3}{x} = y$  to take? Is it a linear or nonlinear function?



9. What shape do you expect the graph of the function described by  $\frac{4}{x^2} = y$  to take? Is it a linear or nonlinear function?



10. What shape do you expect the graph of the equation  $x^2 + y^2 = 36$  to take? Is it a linear or nonlinear? Is it a function? Explain.



**Lesson 8 Summary:**

### Lesson 8 Independent Practice

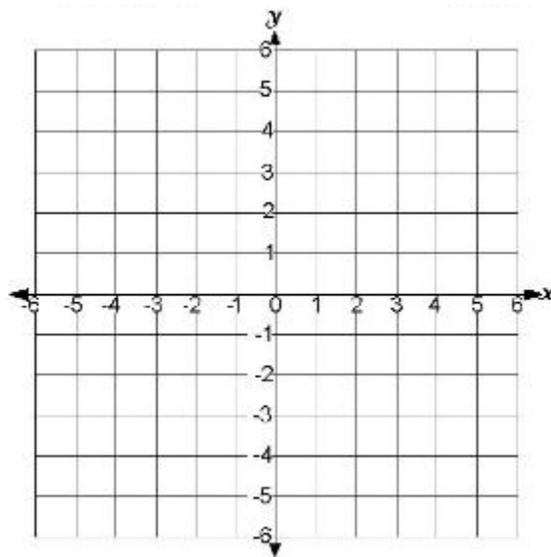
1. A function has the rule so that each input of  $x$  is assigned an output of  $x^2 - 4$ .

a. Do you think the function is linear or nonlinear? Explain.

b. What shape do you expect the graph of the function to be?

c. Develop a list of inputs and outputs for this function. Plot the inputs and outputs as points on the coordinate plane where the output is the  $y$ -coordinate.

Input ( $x$ )	Output ( $x^2 - 4$ )
-3	
-2	
-1	
0	
1	
2	
3	



d. Was your prediction correct?

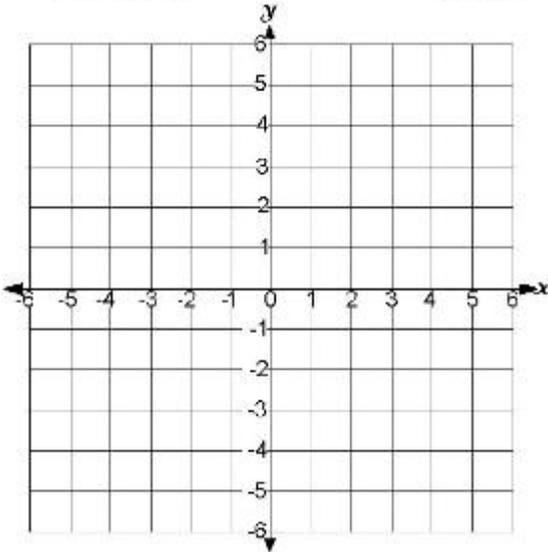
2. A function has the rule so that each input of  $x$  is assigned an output of  $\frac{1}{x+3}$ .

a. Is the function linear or nonlinear? Explain.

b. What shape do you expect the graph of the function to take?

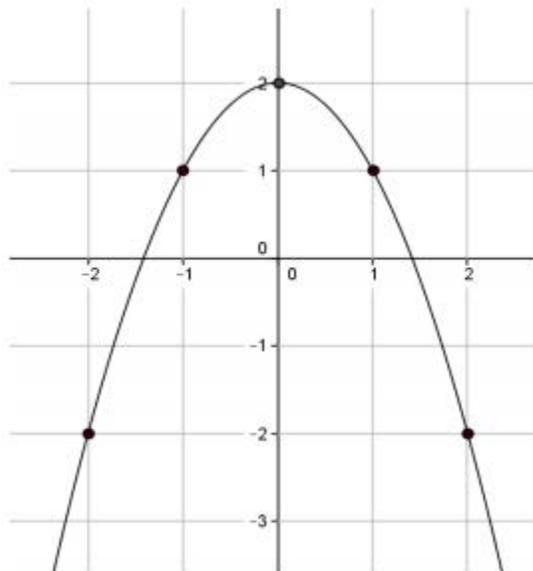
c. Given the inputs in the table below, use the rule of the function to determine the corresponding outputs. Plot the inputs and outputs as points on the coordinate plane where the output is the  $y$ -coordinate.

Input ( $x$ )	Output ( $\frac{1}{x+3}$ )
-2	
-1	
0	
1	
2	
3	



d. Was your prediction correct?

3. Is the function that is represented by this graph linear or nonlinear? Explain. Show work that supports your claim.



## Lesson 9 - Examples of Functions from Geometry

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Essential Questions:

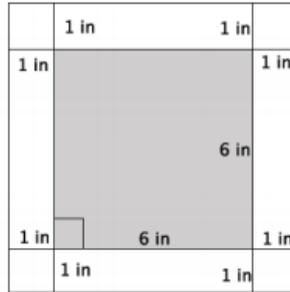
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Exploratory Challenge/On Your Own:

As you complete exercises 1-4, record the information in the following table.

	Side length ( $s$ )	Area ( $A$ )	Expression that describes area of border
Exercise 1			
Exercise 2			
Exercise 3			
Exercise 4			

1. Use the figure below to answer parts (a)-(f).



a. What is the length of one side of the smaller, inner square?

b. What is the area of the smaller, inner square?

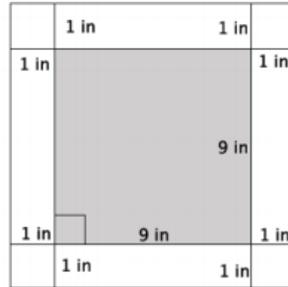
c. What is the length of one side of the larger, outer square?

d. What is the area of the larger, outer square?

e. Use your answers in parts (b) and (d) to determine the area of the 1-inch white border of the figure.

f. Explain your strategy for finding the area of the white border.

2. Use the figure below to answer parts (a)-(f).



a. What is the length of one side of the smaller, inner square?

b. What is the area of the smaller, inner square?

c. What is the length of one side of the larger, outer square?

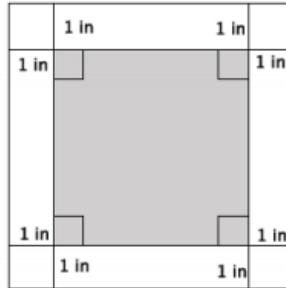
d. What is the area of the larger, outer square?

e. Use your answers in parts (b) and (d) to determine the area of the 1-inch white border of the figure.

f. Explain your strategy for finding the area of the white border.



4. Write a function that would allow you to calculate the area of a 1-inch white border for any sized square picture measured in inches.



a. Write an expression that represents the side length of the smaller, inner square.

b. Write an expression that represents the area of the smaller, inner square.

c. Write an expression that represents the side lengths of the larger, outer square.

d. Write an expression that represents the area of the larger, outer square.

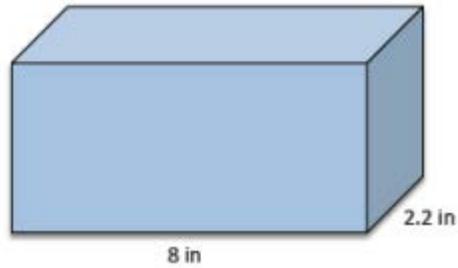
e. Use your expressions in parts (b) and (d) to write a function for the area  $A$  of the 1-inch white border for any sized square picture measured in inches.

**Discussion:**

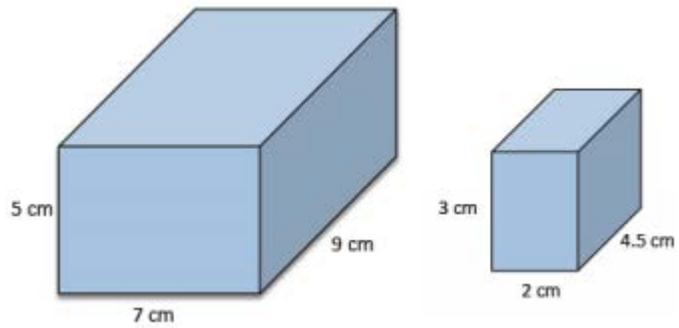
Define Volume:	
Volume Formula:	
Volume Assumptions:	a)  b)  c)  d)

**On Your Own:**

5. The volume of the prism shown is  $61.6 \text{ in}^3$ . What is the height of the prism?



6. Find the value of the ratio that compares the volume of the larger prism to the smaller prism.



**Exploratory Challenge/On Your Own:**

As you complete Exercises 7-10, record the information in the table below. Note that base refers to the bottom of the prism.

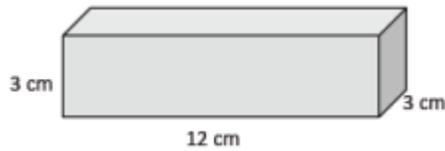
	Area of base ( $B$ )	Height ( $h$ )	Volume
Exercise 7			
Exercise 8			
Exercise 9			
Exercise 10			

7. Use the figure to the right to answer parts (a)-(c).

a. What is the area of the base?

b. What is the height of the figure?

c. What is the volume of the figure?

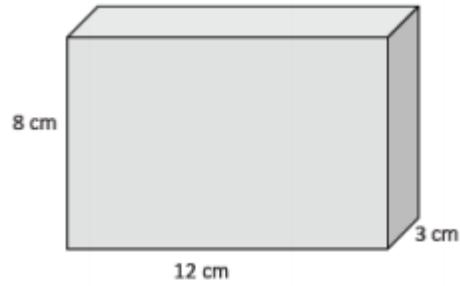


8. Use the figure to the right to answer parts (a)-(c).

a. What is the area of the base?

b. What is the height of the figure?

c. What is the volume of the figure?

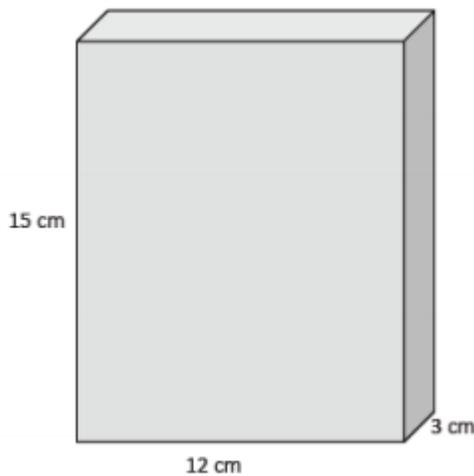


9. Use the figure to the right to answer parts (a)-(c).

a. What is the area of the base?

b. What is the height of the figure?

c. What is the volume of the figure?

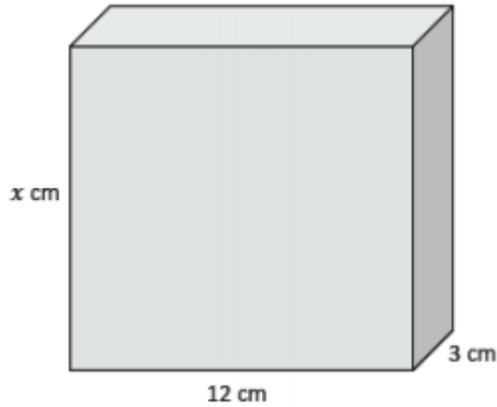


10. Use the figure to the right to answer parts (a)-(c).

a. What is the area of the base?

b. What is the height of the figure?

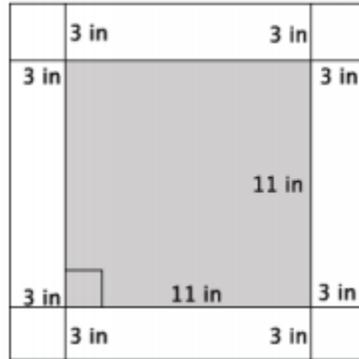
c. Write and describe a function that will allow you to determine the volume of any rectangular prism that has a base area of  $36 \text{ cm}^2$ .



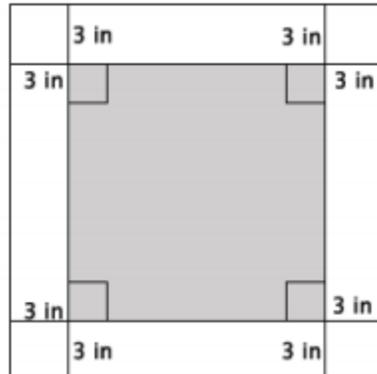
**Lesson 9 Summary:**

**Lesson 9 Independent Practice**

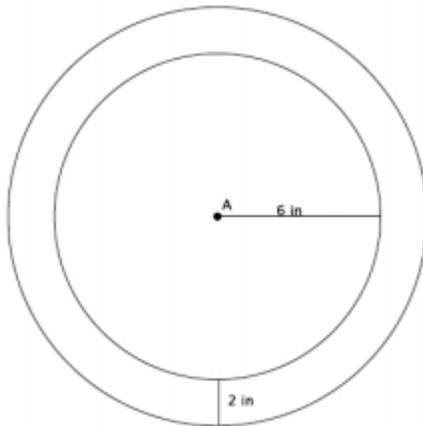
1. Calculate the area of the 3-inch white border of the square figure below.



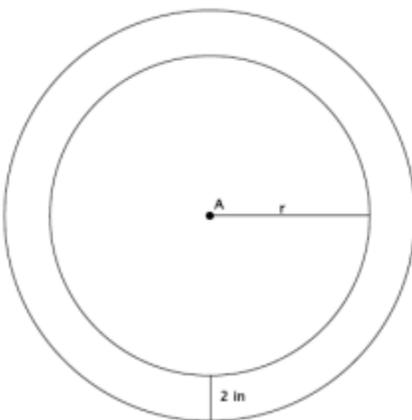
2. Write a function that would allow you to calculate the area,  $A$ , of a 3-inch white border for any sized square picture measured in inches.



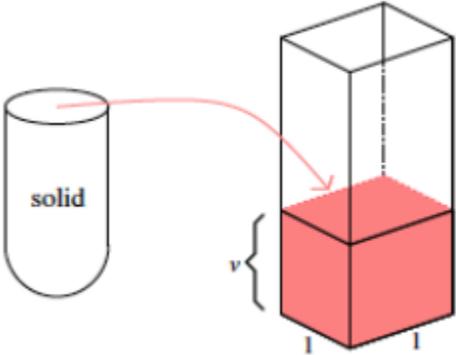
3. Dartboards typically have an outer ring of numbers that represent the number of points a player can score for getting a dart in that section. A simplified dartboard is shown below. The center of the circle is point  $A$ . Calculate the area of the outer ring. Write an exact answer that uses  $\pi$  (do not approximate your answer by using 3.14 for  $\pi$ ).



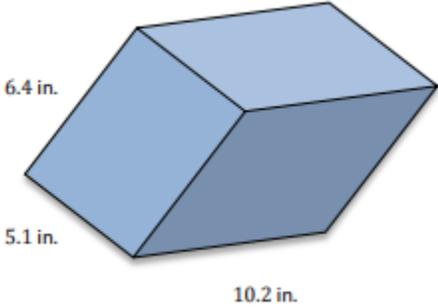
4. Write a function that would allow you to calculate the area,  $A$ , of the outer ring for any sized dartboard with radius  $r$ . Write an exact answer that uses  $\pi$  (do not approximate your answer by using 3.14 for  $\pi$ ).



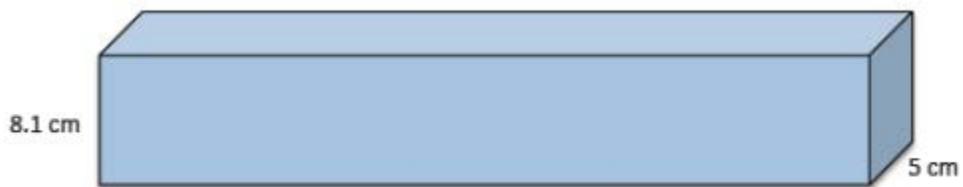
5. The shell of the solid shown was filled with water and then poured into the standard rectangular prism, as shown. The height that the volume reaches is 14.2 in. What is the volume of the solid?



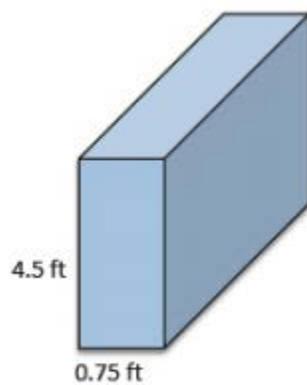
6. Determine the volume of the rectangular prism shown below.



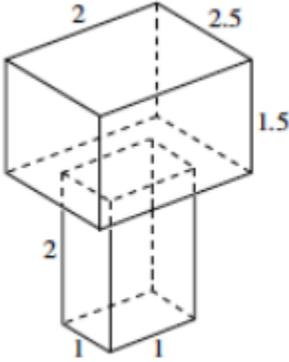
7. The volume of the prism shown below is  $972 \text{ cm}^3$ . What is its length?



8. The volume of the prism shown below is  $32.7375 \text{ ft}^3$ . What is its width?



9. Determine the volume of the 3-dimensional figure below. Explain how you got your answer.



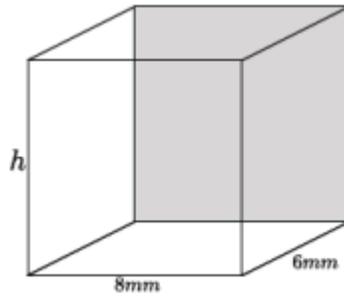
## Lesson 10 - Volumes of Familiar Solids-Cones and Cylinders

Essential Questions:

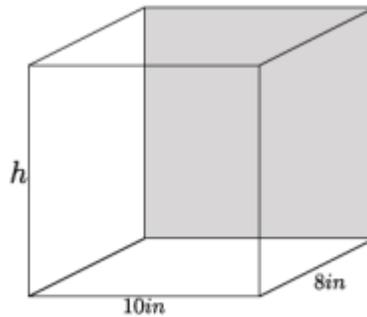
On Your Own:

a.

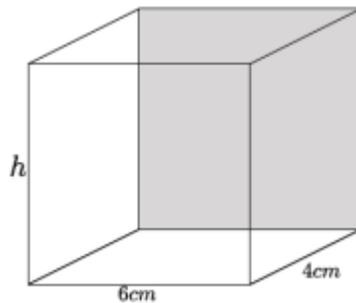
i. Write an equation to determine the volume of the rectangular prism shown.



ii. Write an equation to determine the volume of the rectangular prism shown.

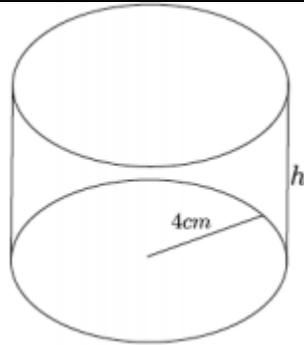


iii. Write an equation to determine the volume of the rectangular prism shown.



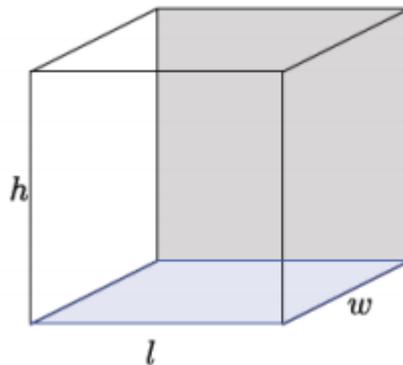
iv. Write an equation for volume,  $V$ , in terms of the area of the base,  $B$ .

b. Using what you learned in part (a), write an equation to determine the volume of the cylinder shown.



**Discussion:**

Volume of Rectangular Prism:



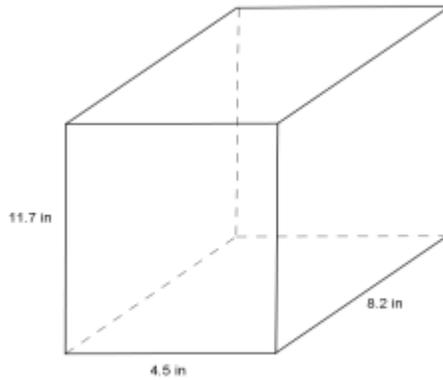
Volume of a Cylinder:



**On Your Own**

1. Use the diagram to answer the questions.

a. What is the area of the base?

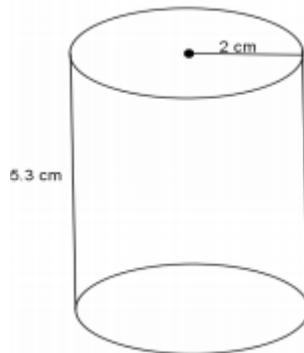


b. What is the height?

c. What is the volume of the rectangular prism?

2. Use the diagram at right to answer the questions.

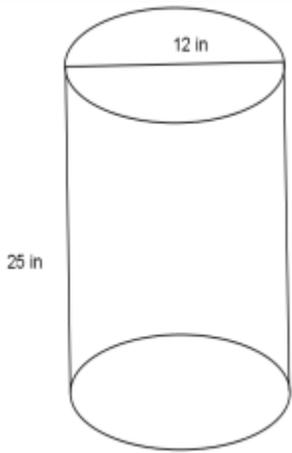
a. What is the area of the base?



b. What is the height?

c. What is the volume of the right circular cylinder?

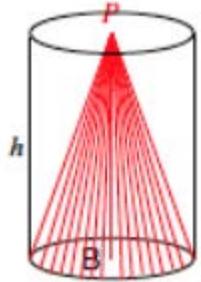
3. Use the diagram at right to answer the questions.  
a. What is the area of the base?



b. What is the height?  
c. What is the volume of the right circular cylinder?

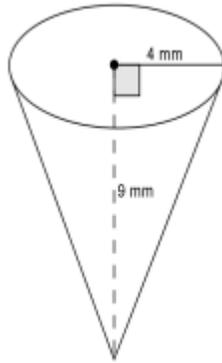
**Discussion**

Volume of a Cone:

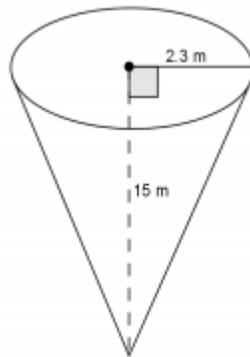


**On Your Own**

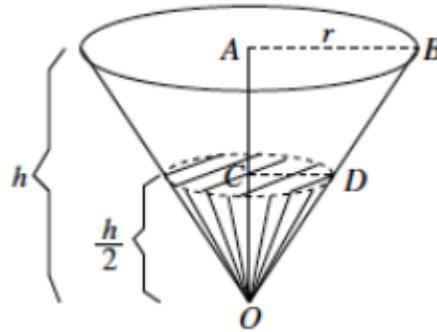
4. Use the diagram to find the volume of the right circular cone.



5. Use the diagram to find the volume of the right circular cone.



6. Challenge: A container in the shape of a right circular cone has height  $h$ , and base of radius  $r$ , as shown. It is filled with water (in its upright position) to half the height. Assume that the surface of the water is parallel to the base of the inverted cone. Use the diagram to answer the following questions:



a. What do we know about the lengths of  $AB$  and  $AO$ ?

b. What do we know about the measure of  $\angle OAB$  and  $\angle OCD$ ?

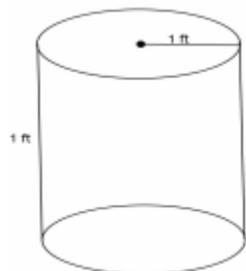
c. What can you say about  $\triangle OAB$  and  $\triangle OCD$ ?

d. What is the ratio of the volume of water to the volume of the container itself?

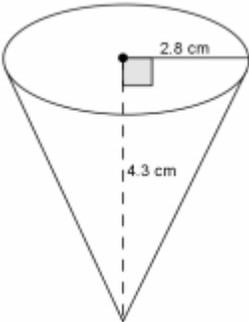
**Lesson 10 Summary:**

**Lesson 10 Independent Practice**

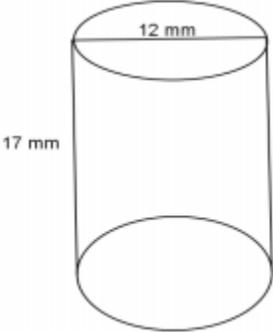
1. Use the diagram to help you find the volume of the right circular cylinder.



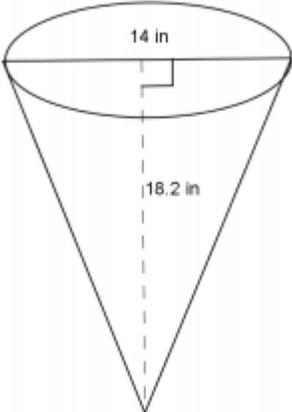
2. Use the diagram to help you find the volume of the right circular cone.



3. Use the diagram to help you find the volume of the right circular cylinder.

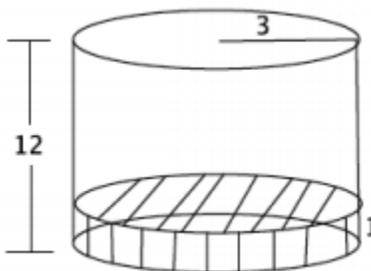


4. Use the diagram to help you find the volume of the right circular cone.



5. Oscar wants to fill with water a bucket that is the shape of a right circular cylinder. It has a 6-inch radius and 12-inch height. He uses a shovel that has the shape of right circular cone with a 3-inch radius and 4-inch height. How many shovelfuls will it take Oscar to fill the bucket up level with the top?

6. A cylindrical tank (with dimensions shown below) contains water that is 1-foot deep. If water is poured into the tank at a constant rate of  $20 \text{ ft}^3/\text{min}$  for 20 min., will the tank overflow? Use 3.14 to estimate  $\pi$ .



## Lesson 11 - Volume of a Sphere

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Essential Questions:

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Discussion:

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On Your Own

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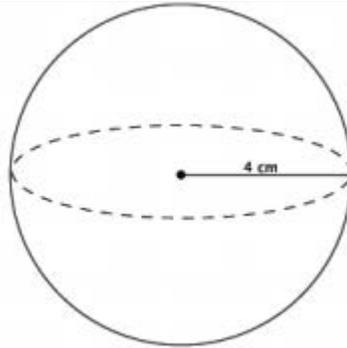
1. What is the volume of a cylinder?

2. What is the height of the cylinder?

3. If  $\text{volume (sphere)} = \frac{2}{3} \text{ volume (cylinder with same diameter and height)}$ , what is the formula for the volume of a sphere?

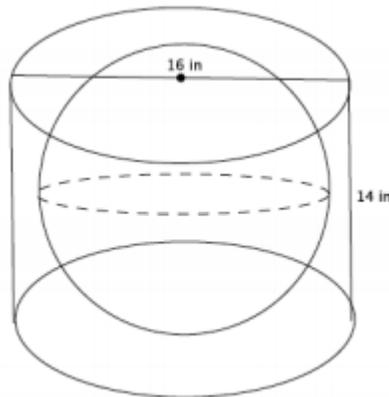
**Example 1**

Compute the exact volume for the sphere shown.



**Example 2**

A cylinder has a diameter of 16 inches and a height of 14 inches. What is the volume of the largest sphere that will fit into the cylinder?



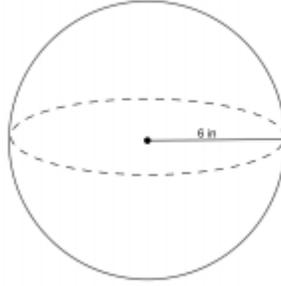
What is the radius of the base of the cylinder?

Could the sphere have a radius of 8 inches? Explain.

Now that we know the radius of the largest sphere is 7 inches. What is the volume of the sphere?

**On Your Own**

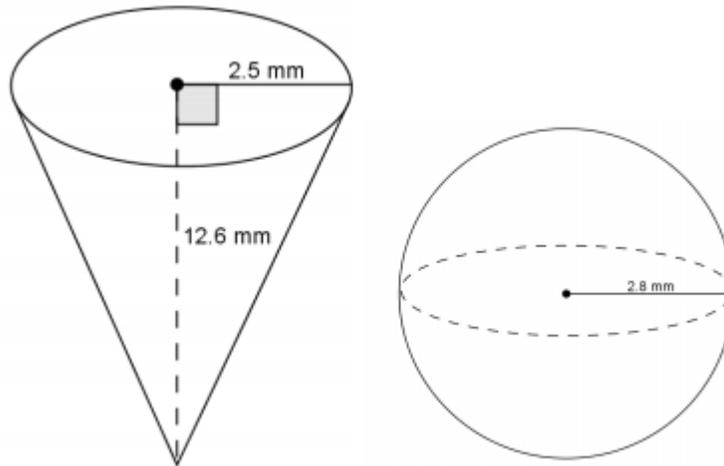
4. Use the diagram and the general formula to find the volume of the sphere.



5. The average basketball has a diameter of 9.5 inches. What is the volume of an average basketball? Round your answer to the tenths place.

6. A spherical fish tank has a radius of 8 inches. Assuming the entire tank could be filled with water, what would the volume of the tank be? Round your answer to the tenths place.

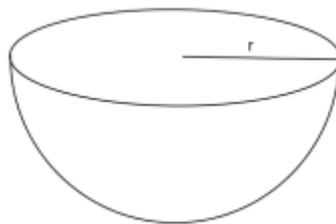
7. Use the diagram to answer the questions.



a. Predict which of the figures shown above has the greater volume. Explain.

b. Use the diagram to find the volume of each, and determine which has the greater volume.

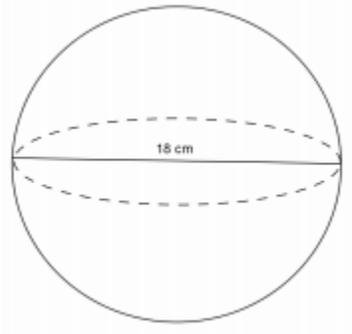
8. One of two half spheres formed by a plane through the sphere's center is called a hemisphere. What is the formula for the volume of a hemisphere?



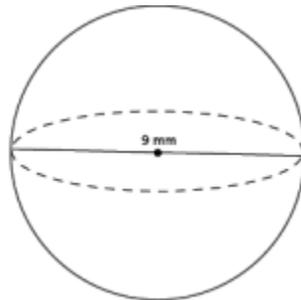
**Lesson 11 Summary:**

**Lesson 11 Independent Practice**

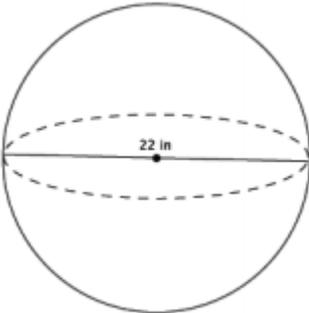
1. Use the diagram to find the volume of the sphere.



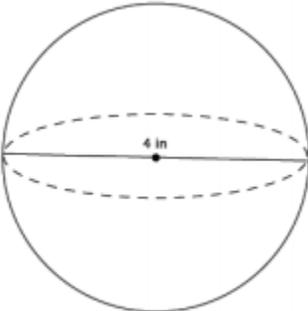
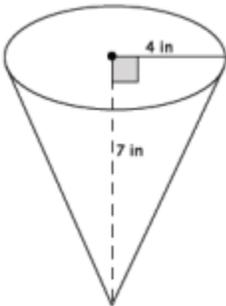
2. Determine the volume of a sphere with diameter 9 mm, shown below.



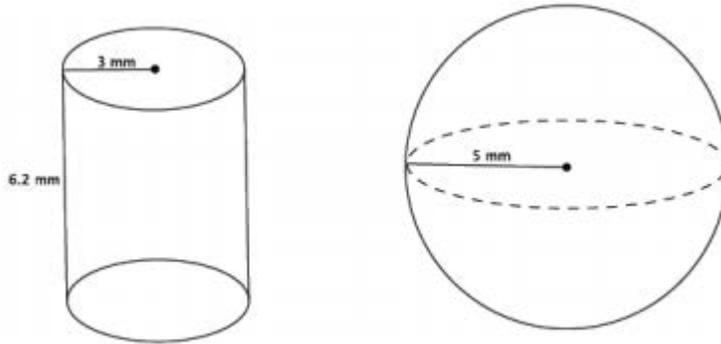
3. Determine the volume of a sphere with diameter 22 in., shown below.



4. Which of the two figures below has the lesser volume?



5. Which of the two figures below has the greater volume?



6. Bridget wants to determine which ice cream option is the best choice. The chart below gives the description and prices for her options. Use the space below each item to record your findings.

\$2.00	\$3.00	\$4.00
1 scoop in a cup	2 scoops in a cup	3 scoops in a cup
Half a scoop on a cone filled with ice cream		A cup filled with ice cream (level to the top of the cup)

A scoop of ice cream is considered a perfect sphere and has a 2-inch diameter. A cone has a 2-inch diameter and a height of 4.5 inches. A cup, considered a right circular cylinder, has a 3-inch diameter and a height of 2 inches.

a. Determine the volume of each choice. Use 3.14 to approximate  $\pi$ .

b. Determine which choice is the best value for her money. Explain your reasoning.