

Coordinate Systems

Instructional Focus: Represent and calculate with vectors

	4 – Mastery	3 – Proficient	2 - Basic	1 – Below Basic	0 – No Evidence
Represent vectors (N.VM.1)	Can extend thinking beyond the standard, including tasks that may involve one of the following:	Use appropriate symbols for vectors and their magnitude, represent vector quantities by directed line segments, and find the magnitude and direction of vector quantities.	Use appropriate symbols for vectors and their magnitude and represent vector quantities by directed line segments.	Use appropriate symbols for vectors and their magnitude	Little evidence of reasoning or application to solve the problem
Solve problems with vectors (N.VM.3)	<ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving 	Solve problems involving velocity and other quantities by converting given direction and magnitude quantities into component vectors, calculate the resultant vector, and find the resultant direction and magnitude or the angle between vectors	Solve problems involving velocity and other quantities by converting given direction and magnitude quantities into component vectors, and calculate the resultant vector	Solve problems involving velocity and other quantities by converting given direction and magnitude quantities into component vectors	Does not meet the criteria in a level 1
Operations with vectors (N.VM.2, N.VM.4, N.VM.5)		Find the components of a vector by subtracting coordinates Add, subtract vectors graphically and component-wise, and determine the magnitude and direction Multiply a vector by a scalar and determine the magnitude and direction	Find the components of a vector by subtracting coordinates Add, subtract vectors graphically and component-wise Multiply a vector by a scalar	Find the components of a vector by subtracting coordinates Add, subtract vectors graphically or component-wise Multiply a vector by a scalar	

N.VM.1 (+) Recognize vector quantities as having both magnitude and direction. Represent vector quantities by directed line segments, and use appropriate symbols for vectors and their magnitudes (e.g., \mathbf{v} , $|\mathbf{v}|$, $||\mathbf{v}||$, v).

N.VM.3 (+) Solve problems involving velocity and other quantities that can be represented by vectors.

N.VM.2 (+) Find the components of a vector by subtracting the coordinates of an initial point from the coordinates of a terminal point.

N.VM.4 (+) Add and subtract vectors.

- a. Add vectors end-to-end, component-wise, and by the parallelogram rule. Understand that the magnitude of a sum of two vectors is typically not the sum of the magnitudes.
- b. Given two vectors in magnitude and direction form, determine the magnitude and direction of their sum.
- c. Understand vector subtraction $\mathbf{v} - \mathbf{w}$ as $\mathbf{v} + (-\mathbf{w})$, where $-\mathbf{w}$ is the additive inverse of \mathbf{w} , with the same magnitude as \mathbf{w} and pointing in the opposite direction. Represent vector subtraction graphically by connecting the tips in the appropriate order, and perform vector subtraction component-wise.

N.VM.5 (+) Multiply a vector by a scalar.

- a. Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise, e.g., as $c(v_x, v_y) = (cv_x, cv_y)$.
- b. Compute the magnitude of a scalar multiple $c\mathbf{v}$ using $||c\mathbf{v}|| = |c|v$. Compute the direction of $c\mathbf{v}$ knowing that when $|c|v \neq 0$, the direction of $c\mathbf{v}$ is either along \mathbf{v} (for $c > 0$) or against \mathbf{v} (for $c < 0$).

Coordinate Systems

Instructional Focus: Represent and calculate complex numbers

	4 – Mastery	3 – Proficient	2 - Basic	1 – Below Basic	0 – No Evidence
Represent on the complex plane (N.CN.4)	Can extend thinking beyond the standard, including tasks that may involve one of the following: <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving 	Represent complex numbers on the complex plane in rectangular and polar form, and explain why the rectangular and polar forms of a given complex number represent the same number	Represent complex numbers on the complex plane in rectangular and polar form	Represent complex numbers on the complex plane in rectangular form	Little evidence of reasoning or application to solve the problem
Operations of Vectors in Polar Form (N.CN.3, N.CN.5)		Represent and compute addition and subtraction of complex numbers geometrically on the complex plane Represent and compute multiplication and division, in polar form, of complex numbers geometrically on the complex plane Represent and compute the power and roots of complex numbers, in polar form.	Represent and compute addition and subtraction of complex numbers geometrically on the complex plane Represent and compute multiplication and division, in polar form, of complex numbers geometrically on the complex plane	Represent and compute addition and subtraction of complex numbers geometrically on the complex plane	Does not meet the criteria in a level 1
Calculate distance and midpoint (N.CN.6)		Calculate the distance between numbers in the complex plane as the modulus of the difference , and calculate the midpoint of a segment in the complex plane as the average of the numbers at its endpoints	Calculate the difference between numbers in the complex plane , and calculate the midpoint of a segment in the complex plane as the average of the numbers at its endpoints	Calculate the midpoint of a segment in the complex plane as the average of the numbers at its endpoints	

N.CN.4 (+) Represent complex numbers on the complex plane in rectangular and polar form (including real and imaginary numbers), and explain why the rectangular and polar forms of a given complex number represent the same number.

N.CN.3 (+) Find the conjugate of a complex number; use conjugates to find moduli and quotients of complex numbers.

N.CN.5 (+) Represent addition, subtraction, multiplication, and conjugation of complex numbers geometrically on the complex plane; use properties of this representation for computation. *For example, $(-1 + \sqrt{3}i)^3 = 8$ because $(-1 + \sqrt{3}i)$ has modulus 2 and argument 120° .*

N.CN.6 (+) Calculate the distance between numbers in the complex plane as the modulus of the difference, and the midpoint of a segment as the average of the numbers at its endpoints.

Limits

Instructional Focus: Find limits and continuity

	4 – Mastery	3 – Proficient	2 - Basic	1 – Below Basic	0 – No Evidence
Find limits	Can extend thinking beyond the standard, including tasks that may involve one of the following:	Find limits and one-sided limits graphically, numerically, and algebraically, using proper notation. Describe end behavior (as x approaches or $-$) using limit notation	Find limits and one-sided limits graphically and numerically. Describe end behavior (as x approaches ∞ or $-\infty$) using limit notation.	Find limits and one-sided limits graphically and numerically	Little evidence of reasoning or application to solve the problem
Determine continuity	<ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving 	<p>Determine continuity of functions graphically, numerically, and algebraically on its domain using the three-part definition of continuous functions.</p> <p>Determine values for which a function is discontinuous, understand the difference between removable and nonremovable discontinuities, and be able to redefine functions to make them continuous when possible.</p> <p>Find finite and infinite one-sided limits, and describe asymptotes using limit notation.</p>	<p>Determine continuity of functions graphically and numerically on its domain using the three-part definition of continuous functions.</p> <p>Determine values for which a function is discontinuous, and understand the difference between removable and nonremovable discontinuities.</p> <p>Find finite and infinite one-sided limits.</p>	<p>Determine continuity of functions graphically and numerically at a given value using the three-part definition of continuous functions.</p> <p>Determine values for which a function is discontinuous.</p> <p>Determine whether a one-sided limit is finite or infinite.</p>	Does not meet the criteria in a level 1

Find limits and one-sided limits graphically, numerically, and algebraically, using proper notation. Describe end behavior (as x approaches or $-$) using limit notation.

Determine continuity of functions graphically, numerically, and algebraically on its domain using the three-part definition of continuous functions. Determine values for which a function is discontinuous, understand the difference between removable and nonremovable discontinuities, and be able to redefine functions to make them continuous when possible. Find finite and infinite one-sided limits, and describe asymptotes using limit notation.